



Univerza v Mariboru

Fakulteta za naravoslovje
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

| | |
|----------------------|----------------------------|
| Predmet: | Nelinearna dinamika |
| Course title: | Nonlinear dynamics |

| Študijski program in stopnja Study programme and level | Študijska smer Study field | Letnik Academic year | Semester Semester |
|--|--------------------------------------|-----------------------------------|-----------------------------|
| FIZIKA, 3. stopnja | | 1. ali 2. | 1., 2. ali 4. |
| PHYSICS, 3 rd cycle | | 1. or 2. | 1., 2. or 4. |

Vrsta predmeta / Course type

Izbirni za vse module

Univerzitetna koda predmeta / University course code:

| Predavanja Lectures | Seminar Seminar | Vaje Tutorial | Lab. vaje Laboratory work | Mentorstvo Mentorship | Samost. delo Individ. work | ECTS |
|-------------------------------|---------------------------|-------------------------|--|---------------------------------|---|-------------|
| 10 | 5 | | | | 165 | 6 |

Nosilec predmeta / Lecturer:

Marko Robnik

**Jeziki /
Languages:**

**Predavanja /
Lectures:** slovenski/Slovenian in/and angleški s slovenskim
prevodom/English with translation in Slovenian
Vaje / Tutorial:

**Pogoji za vključitev v delo oz. za opravljanje
študijskih obveznosti:**

Ni posebnih zahtev.

Prerequisites:

No special prerequisites.

Vsebina:

Content (Syllabus outline):

Uvod v dinamiko:

- Avtonomni dinamični sistemi prvega reda
- Linearne transformacije ravnine
- Avtonomni dinamični sistemi drugega reda
- Konservativni hamiltonski sistemi z eno prostostno stopnjo
- Lagrangiani
- Teorije transformacij
- Kotne in akcijske spremenljivke
- Teorije motenj
- Adiabatični in hitri oscilirajoči pogoji
- Linearni sistemi
- Kaotično gibanje in nelinearne preslikave

Uvod v nelinearno dinamiko:

- Uvod in pregled
- Enodimenzionalne preslikave
- Čudni atraktorji (strange attractors) in fraktalna dimenzija
- Dinamične lastnosti kaotičnih sistemov
- Kaotične množice, ki niso atraktorji
- Kvaziperiodičnost
- Kaos v hamiltonskih sistemih
- Kaotični prehodi
- Multifraktali
- Kvantni kaos

Introduction to dynamics:

- Autonomous dynamical systems of first order
- Linear transformations in the plane
- Autonomous dynamical systems of second order
- Conservative Hamiltonian systems with one degree of freedom
- Lagrangians
- Theory of transformations
- Angle and action variables
- Perturbation theory
- Adiabatic and fast oscillations conditions
- Linear systems
- Chaotic motion and nonlinear mapping

Introduction to nonlinear dynamics:

- Introduction and overview
- Onedimensional mappings
- Strange attractors and fractal dimension
- Dynamical properties of chaotic systems
- Chaotic sets, which are not strange attractors
- Quasiperiodicity
- Chaos in Hamiltonian systems
- Chaotic transitions
- Multifractals
- Quantum chaos

Temeljni literatura in viri / Readings:

1) Percival, I., & Richards, D. (1991). *Introduction to Dynamics* (Repr., str. 228). Cambridge University Press. <https://plus.cobiss.net/cobiss/si/sl/bib/pefmb/3471112> 2) Ott, E. (1993/2000, cop.). *Chaos in dynamical systems* (Reprinted, str. XII, 385). Cambridge University Press. <https://plus.cobiss.net/cobiss/si/sl/bib/pefmb/11369224>

Dodatna:

Lichtenberg, A. J., & Leiberman, M. A. (1983). *Regular and stochastic motion*. Springer.

LOZEJ, Črt, LUKMAN, Dragan, ROBNIK, Marko. Effects of stickiness in the classical and quantum ergodic lemon billiard. *Physical review. E.*, ISSN 2470-0053, 2021, vol. 103, issue 1, str. 1-12, graf. prikazi, tabele, doi: 10.1103/PhysRevE.103.012204

Cilji in kompetence:

Objectives and competences:

- Razumeti osnove nelinearne dinamike
- Pridobiti osnovne izkušnje pri uporabi metod nelinearne dinamike
- Rešiti nekaj osnovnih problemov s področja nelinearne dinamike v okviru seminarske naloge

- Understanding the fundamentals of nonlinear dynamics
- Gaining the basic experience in applying the methods of nonlinear dynamics
- Solving some fundamental problems in the field of nonlinear dynamics as a seminar report

Predvideni študijski rezultati:

Znanje in razumevanje:

- Znanje osnov nelinearne dinamike
- Poglobljeno razumevanje principov nelinearne dinamike

Prenesljive/ključne spretnosti in drugi atributi:

- Sposobnost uporabe metod nelinearne dinamike
- Uporaba metod na drugih aplikativnih področjih
- Samostojno razvijanje fizikalnega znanja

Intended learning outcomes:

Knowledge and understanding:

- Knowledge of the fundamentals of nonlinear dynamics
- Understanding the principles of nonlinear dynamics

Transferable/Key Skills and other attributes:

- Capability of applying the methods of nonlinear dynamics
- Application of methods in other applied fields
- Development of new knowledge

Metode poučevanja in učenja:

Predavanja, seminar

Learning and teaching methods:

Lectures, seminar

Načini ocenjevanja:

Način (pisni izpit, ustno izpraševanje, naloge, projekt)

- Ustni izpit
- Pisni izpit

Delež (v %) /

Weight (in %)

Assessment:

Type (examination, oral, coursework, project):

- Oral exam
- Written exam

Reference nosilca / Lecturer's references:

1. GRUBELNIK, Vladimir, LOGAR, Marjan, ROBNIK, Marko. Quantum Fermi acceleration in the resonant gaps of a periodically driven one-dimensional potential box. *Journal of physics. A, Mathematical and theoretical*, ISSN 1751-8113, 2014, vol. 47, no. 35, str. 355103-1 - 355103-17, doi: [10.1088/1751-8113/47/35/355103](https://doi.org/10.1088/1751-8113/47/35/355103). [COBISS.SI-ID [18017814](https://www.cobiss.si/id/18017814)]
2. MANOS, Thanos, ROBNIK, Marko. Survey on the role of accelerator modes for anomalous diffusion : the case of the standard map. *Physical review. E, Statistical, nonlinear and soft matter physics*, ISSN 1550-2376. [Online ed.], 2014, vol. 89, iss. 2, str. 022905-1 - 022905-12, graf. prikazi, doi: [10.1103/PhysRevE.89.022905](https://doi.org/10.1103/PhysRevE.89.022905). [COBISS.SI-ID [77280257](https://www.cobiss.si/id/77280257)]

3. ANDRESAS, Dimitris, BATISTIĆ, Benjamin, ROBNIK, Marko. Statistical properties of one-dimensional parametrically kicked Hamilton systems. *Physical review. E, Statistical, nonlinear, and soft matter physics*, ISSN 1539-3755, 2014, vol. 89, no. 6, str. 062927-1-062927-14, graf. prikazi, doi: [10.1103/PhysRevE.89.062927](https://doi.org/10.1103/PhysRevE.89.062927). [COBISS.SI-ID 78977281]
4. BATISTIĆ, Benjamin, MANOS, Thanos, ROBNIK, Marko. The intermediate level statistics in dynamically localized chaotic eigenstates. *Europhysics letters*, ISSN 0295-5075, 2013, vol. 102, no. 5, str. 50008-1-50008-6. http://iopscience.iop.org/0295-5075/102/5/50008/pdf/0295-5075_102_5_50008.pdf, doi: [10.1209/0295-5075/102/50008](https://doi.org/10.1209/0295-5075/102/50008). [COBISS.SI-ID 74806017]
5. BATISTIĆ, Benjamin, ROBNIK, Marko. Dynamical localization of chaotic eigenstates in the mixed-type systems: spectral statistics in a billiard system after separation of regular and chaotic eigenstates. *Journal of physics. A, Mathematical and theoretical*, ISSN 1751-8113, 2013, vol. 46, no. 31, str. 315102-1-315102-17. http://iopscience.iop.org/1751-8113/46/31/315102/pdf/1751-8113_46_31_315102.pdf, doi: [10.1088/1751-8113/46/31/315102](https://doi.org/10.1088/1751-8113/46/31/315102). [COBISS.SI-ID 75147009]
6. MANOS, Thanos, ROBNIK, Marko. Dynamical localization in chaotic systems: spectral statistics and localization measure in the kicked rotator as a paradigm for time-dependent and time-independent systems. *Physical review. E, Statistical, nonlinear and soft matter physics*, ISSN 1550-2376. [Online ed.], 2013, vol. 87, iss. 6, str. 062905-1 - 062905-17, graf. prikazi. <http://pre.aps.org/pdf/PRE/v87/i6/e062905>, doi: [10.1103/PhysRevE.87.062905](https://doi.org/10.1103/PhysRevE.87.062905). [COBISS.SI-ID 74771713]