



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

### UČNI NAČRT PREDMETA / COURSE SYLLABUS

<b>Predmet:</b>	Nelinearni dinamični sistemi
<b>Course title:</b>	Nonlinear Dynamical Systems

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester
Fizika 2. st. Physics 2 <sup>nd</sup> degree		1	2

**Vrsta predmeta / Course type**

**Univerzitetna koda predmeta / University course code:**

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
15		30			105	5

**Nosilec predmeta / Lecturer:**

<b>Jeziki /</b>	<b>Predavanja / Lectures:</b>	slovenski/Slovenian
<b>Languages:</b>	<b>Vaje / Tutorial:</b>	slovenski/Slovenian

**Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:**

**Prerequisites:**

**Vsebina:**

**Content (Syllabus outline):**

<p><b>1. Nelinearni dinamični sistemi v 1D, 2D in 3D</b> Linearizacija in linearna stabilnostna analiza, bifurkacijska analiza.</p> <p><b>2. Nelinearni oscilatorji</b> Regularni oscilatorji kot konzervativni in disipativni sistemi (center, limitni cikel), bifurkacije, bifurkacijski diagram, lokalne in globalne bifurkacije.</p> <p><b>3. Kvaziperiodičnost, kaos</b> Fourierjeva transformacija in avtokorelacija, Lyapunovi eksponenti, kaos, fraktali in fraktalne dimenzije.</p> <p><b>4. Fraktali in fraktalne dimenzije.</b></p> <p><b>5. Stohastično modeliranje</b> (Gillespiev algoritem)</p> <p><b>6. Aplikacije</b> Pomen dinamičnih sistemov v fiziki in na drugih področjih: dinamični sistemi v biologiji, okoljevarstvu, ekonomiji, ....</p> <p><b>7. Uporaba računalniških programov</b> Uporaba računalniških programov za implementacijo dinamičnih sistemov: DynaSys, Stella, Madonna, C++, ...</p>
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<p><b>1. Nonlinear dynamical systems (1D-, 2D-, 3D-systems)</b> Linearization and the linear stability analysis, the bifurcation analysis.</p> <p><b>2. Nonlinear oscillators</b> Regular oscillators as conservative and dissipative systems (centre, limit cycle), bifurcations, bifurcation diagram, local and global bifurcations.</p> <p><b>3. Quasiperiodicity, chaos</b> Fourier transformation and autocorrelation, Lyapunov exponents, chaos, fractals and fractal dimensions.</p> <p><b>4. Fractals and fractal dimension</b></p> <p><b>5. Stochastic modelling</b> (Gillespie's algorithm)</p> <p><b>6. Applications</b> The role of dynamical systems in physics and in other fields: dynamical systems in biology, environmental science, economy, ...</p> <p><b>7. Using of computer programs</b> Computer programmes for the implementation of dynamical systems: DynaSys, Stella, Madonna, C++, ...</p>
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**Temeljni literatura in viri / Readings:**

<ol style="list-style-type: none"> <li>1. Steven H. Strogatz, Nonlinear Dynamics and Chaos with Applications to Physics, Biology, Chemistry, and Engineering. Perseus Pub., Cambridge, 1994.</li> <li>2. J. B. Snape, I. J. Dunn, J. Ingham, J. E. Prenosil, Dynamics of Environmental Bioprocesses, Modelling and Simulation, VCH Verlagsgesellschaft, Weinheim, 1995.</li> <li>3. Natali Hritonenko, Yuri Yatsenko, Mathematical Modeling in Economics, Ecology and the Environment, Springer, New York, 1999.</li> <li>4. Strokovni in znanstveni članki v revijah / Articles published in professional and scientific journals.</li> </ol>
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**Cilji:**

**Objectives:**

- Študentje bodo znali kvantitativno analizirati dinamiko kompleksnih sistemov.
- Študentje bodo razumeli ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Uporabiti znanje o dinamičnih sistemih v naravnih sistemih in drugih področjih.
- Uporaba računalniških programov za implementacijo dinamičnih sistemov.

- Students will be able to quantitative analyse the dynamics of complex systems.
- Students will be able to understand basic differences and characteristics of dynamical systems in different dimensions.
- Using knowledge about dynamical systems in the nature and the other fields.
- Using computer programs for the implementation of dynamical systems.

#### Predvideni študijski rezultati:

##### Znanje in razumevanje:

- Uporabiti pridobljeno znanje pri kvantitativni analizi dinamike kompleksnih sistemov.
- Razložiti ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Razumeti deterministično in stohastično modeliranje.
- Uporabiti znanje o dinamičnih sistemih v fiziki in prenos znanja na druga področja.
- Znati uporabljati računalniške programe za implementacijo dinamičnih sistemov.

##### Prenesljive/ključne spretnosti in drugi atributi:

- Metode kvantitativne analize dinamičnih sistemov so univerzalne in jih je mogoče uporabiti na najrazličnejših področjih.
- Poudarek je na prenosu znanja s primerov iz fizike na področja biologije, ekologije, ekonomije, ...

#### Intended learning outcomes:

##### Knowledge and Understanding:

- apply this knowledge at quantitative analysis of the dynamics of complex systems.
- explain the basic differences and characteristics of dynamical systems in different dimensions.
- Understand the deterministic and stochastic modelling.
- Apply the knowledge about dynamical systems in physics to other fields.
- Using computer programs for the implementation of dynamical systems.

##### Transferable/Key Skills and other attributes:

- Methods for quantitative analysis of dynamical system are universal and can be implemented in different fields of research.
- In particular, a knowledge transfer from examples in physics to examples in biology, ecology, economics, etc. is emphasised.

#### Metode poučevanja in učenja:

- Predavanja
- Teoretične vaje
- Vaje na računalniku
- Eksperimentalno delo

#### Learning and teaching methods:

- Lectures
- Theoretical exercises
- Computer exercises
- Experimental work

#### Načini ocenjevanja:

Delež (v %) /

#### Assessment:

Weight (in %)

• izpit iz teoretičnih znanj	50	• exam of theoretical knowledge
• projektna naloga	50	• project work

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**Reference nosilca / Lecturer's references:**

- OSRAJNIK, Damjan, GRUBELNIK, Vladimir, REPNIK, Robert. Multirhythmicity but no deterministic chaos in vibrating strings. *Chaos, solitons and fractals*. [Print ed.]. Sep. 2021, vol. 150, str. 1-5. DOI: [10.1016/j.chaos.2021.111206](https://doi.org/10.1016/j.chaos.2021.111206). [COBISS.SI-ID [73698819](#)]
- GRUBELNIK, Vladimir, ZMAZEK, Jan, MARKOVIČ, Rene, GOSAK, Marko, MARHL, Marko. Modelling of energy-driven switch for glucagon and insulin secretion. *Journal of theoretical biology*. 2020, vol. 493, str. 1-13, ilustr. ISSN 0022-5193. DOI: [10.1016/j.jtbi.2020.110213](https://doi.org/10.1016/j.jtbi.2020.110213). [COBISS.SI-ID [25173256](#)]
- MARKOVIČ, Rene, GOSAK, Marko, GRUBELNIK, Vladimir, MARHL, Marko, VIRTIČ, Peter. Data-driven classification of residential energy consumption patterns by means of functional connectivity networks. *Applied energy*, ISSN 0306-2619, 2019, vol. 242, str. 506-515, graf. prikazi, doi: [10.1016/j.apenergy.2019.03.134](https://doi.org/10.1016/j.apenergy.2019.03.134). [COBISS.SI-ID [1024346460](#)]
- MARKOVIČ, Rene, GOSAK, Marko, PERC, Matjaž, MARHL, Marko, GRUBELNIK, Vladimir. Applying network theory to fables : complexity in Slovene belles-lettres for different age groups. *Journal of complex networks*, ISSN 2051-1329. [Online ed.], 2019, vol. 7, issue 1, str. 114-127, doi: [10.1093/comnet/cny018](https://doi.org/10.1093/comnet/cny018). [COBISS.SI-ID [24086536](#)]
- GRUBELNIK, Vladimir, LOGAR, Marjan, ROBNIK, Marko, XIA, Yong-Hui. Analysis of the parametrically periodically driven classical and quantum linear oscillator. *Physical review. E.*, ISSN 2470-0053, Feb. 2019, vol. 99, issue 2, str. 022209-1 - 022209-14, graf. prikazi, tabele, doi: [10.1103/PhysRevE.99.022209](https://doi.org/10.1103/PhysRevE.99.022209). [COBISS.SI-ID [96173569](#)]
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