



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

### UČNI NAČRT PREDMETA / COURSE SYLLABUS

<b>Predmet:</b>	Fraktali
<b>Course title:</b>	Fractals

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Enovit magistrski študijski program druge stopnje Predmetni učitelj	/	3. ali / or 4.	6. ali / or 8.
Five-year master's degree program Subject Teacher	/		

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
30	-	15	-	-	45	3

Nosilec predmeta / Lecturer:

Jeziki / Predavanja / Lectures:   
Languages: Vaje / Tutorial:

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Vsebina:

Prerequisites:

Content (Syllabus outline):

- Metrični prostor, različne vrste podprostorov, prostor fraktalov.
- Afine transformacije, skrčitve, sistemi iterirajočih funkcij.
- Teoretično in eksperimentalno določanje dimenzije fraktala, Hausdorff-Bezikovičeva dimenzija.

- A metric space, different types of subspaces, the space of fractals.
- Affine transformations, contraction mappings, systems of iterating functions.
- The theoretical and experimental determination of the fractal dimension, Hausdorff-Besicovitch dimension.

### Temeljni literatura in viri / Readings:

K. J. Falconer: Fractal Geometry. J. Wiley, Chichester (1990)

Y. Pesin, V. Climenhaga: Elements of Fractal Geometry and Dynamics, spletni vir:  
<https://www.math.uh.edu/~climenna/doc/fractals.pdf>

Y. Pesin, V. Climenhaga: Lectures on Fractal Geometry and Dynamical Systems, American Mathematical Society (2009)

J. Vrabec: Metrični prostori. Ljubljana: DMFA (1993).

H. Zeitler, D. Pagon: Fraktale Geometrie: eine Einführung, Vieweg, Braunschweig (2000)

### Cilji in kompetence:

Študenti se seznanijo s strukturo podprostora fraktalov v metričnem prostoru in z osnovnimi načini generiranja fraktalov (družine iterirajočih preslikav). Spoznajo tudi nekaj glavnih definicij dimenzije fraktala.

### Objectives and competences:

Students get familiar with the structure of the subset of fractals in a metric space and with the main ways of generating fractals (iterated functions systems). They also learn the main definitions of the dimension of a fractal set.

### Predvideni študijski rezultati:

Znanje in razumevanje:

- aktivno obvladanje strukture metričnega prostora in prepoznavanje fraktalnih podmnožic
- sposobnost generiranja fraktalov
- teoretično in eksperimentalno določanje dimenzije fraktalov

### Intended learning outcomes:

Knowledge and understanding:

- active knowledge of metric space structure and the ability to recognize its fractal subsets
- the ability to generate fractals
- theoretical and experimental ways to find the dimension of a fractal

### Metode poučevanja in učenja:

### Learning and teaching methods:

<ul style="list-style-type: none"> <li>• Predavanja</li> <li>• Seminarske vaje</li> <li>• Individualno delo</li> </ul>	<ul style="list-style-type: none"> <li>• Lectures</li> <li>• Exercises</li> <li>• Individual work</li> </ul>
--	--

Delež (v %) /

**Načini ocenjevanja:**

Weight (in %)

**Assessment:**

<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt):</p> <ul style="list-style-type: none"> <li>• pisni izpit – praktični del</li> <li>• ustni izpit – teoretični del</li> </ul> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p> <p>Positivna ocena pri pisnem testu je pogoj za pristop k ustnem izpitu.</p>	<p>50%</p> <p>50%</p>	<p>Type (examination, oral, coursework, project):</p> <ul style="list-style-type: none"> <li>• written exam – practical part</li> <li>• oral exam – theoretical part</li> </ul> <p>Each of the mentioned commitments must be assessed with a passing grade.</p> <p>Passing grade of the written test is required for taking the oral exam.</p>
--	-----------------------	--

**Reference nosilca / Lecturer's references:**

1. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Jordan  $\{g,h\}\{\diamond,h\}$ -derivations of unital algebras. *Operators and matrices*. 2022, vol. 16, no. 2, str. 415-428. ISSN 1846-3886. <http://oam.ele-math.com/16-32/Jordan-g,h-derivations-of-unital-algebras>, DOI: [10.7153/oam-2022-16-32](https://doi.org/10.7153/oam-2022-16-32). [COBISS.SI-ID [114972163](https://www.cobiss.si/id/114972163)],
2. XIA, Yong-Hui, GRAŠIČ, Mateja, HUANG, Wentao, ROMANOVSKI, Valery. Limit cycles in a model of olfactory sensory neurons. *International journal of bifurcation and chaos in applied sciences and engineering*. 2019, vol. 29, no. 3, str. 1950038-1-1950038-9. ISSN 0218-1274. DOI: [10.1142/S021812741950038X](https://doi.org/10.1142/S021812741950038X). [COBISS.SI-ID [22250006](https://www.cobiss.si/id/22250006)],
3. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Generalized skew derivations on triangular algebras determined by action on zero products. *Communications in algebra*. 2018, vol. 46, iss. 5, str. 1859-1867. ISSN 0092-7872. <https://doi.org/10.1080/00927872.2017.1360334>, DOI: [10.1080/00927872.2017.1360334](https://doi.org/10.1080/00927872.2017.1360334). [COBISS.SI-ID [18505817](https://www.cobiss.si/id/18505817)].