



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

### UČNI NAČRT PREDMETA / COURSE SYLLABUS

|                      |                      |
|----------------------|----------------------|
| <b>Predmet:</b>      | Matematične krivulje |
| <b>Course title:</b> | Mathematical Curves  |

| Študijski program in stopnja<br>Study programme and level              | Študijska smer<br>Study field | Letnik<br>Academic year | Semester      |
|--|-------------------------------|-------------------------|---------------|
| Enovit magistrski študijski program<br>druge stopnje Predmetni učitelj | /                             | 3. ali/or 4.            | 6. ali /or 8. |
| Five-year master's degree program<br>Subject Teacher                   | /                             |                         |               |

Vrsta predmeta / Course type

Izbirni / Elective

Univerzitetna koda predmeta / University course code:

| Predavanja<br>Lectures | Seminar<br>Seminar | Sem. vaje<br>Tutorial | Lab. vaje<br>Laboratory work | Teren. vaje<br>Field work | Samost. delo<br>Individ. work | ECTS |
|------------------------|--------------------|-----------------------|------------------------------|---------------------------|-------------------------------|------|
| 15                     | 15                 | 15                    |                              |                           | 45                            | 3    |

Nosilec predmeta / Lecturer:

Matevž ČREPNIJAK

Jeziki /

Predavanja / Lectures: slovenski / Slovenian

Languages:

Vaje / Tutorial: slovenski / Slovenian

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Prerequisites:

Opravljen izpit iz Osnov analize in Analize

Exam in Basic Analysis, Analysis

**Vsebina:**

- Krivulje v ravnini. Sistematizacija krivulj.
- Parametrizacija, tangenta, locna dolžina.
- Primeri ravninskih krivulj: stožnice, krivulje tretje stopnje, krivulje četrte stopnje, cikloidne krivulje, transcendentne krivulje.
- Singularna točka. Ogrinjaca.
- Šestnajsti Hilbertov problem.

**Content (Syllabus outline):**

- Planar curves. Systematization of curves.
- Parametrization, tangent, arc length.
- Examples of planar curves: curves of degree 2, curves of degree 3, curves of degree 4, cyclic curves, transcendental curves.
- Singular point. Hull.
- Hilbert's sixteenth problem

**Temeljni literatura in viri / Readings:**

M. Razpet: *Ravninske krivulje*. Ljubljana: Knjižnica sigma, DMFA, 1998.

I. Vidav: *Eliptične krivulje in eliptične funkcije*. Ljubljana: DMFA, 1991.

M. Dobovišek: *Rešene naloge iz analize II*. Ljubljana: DMFA, 1996.

B. Hvala: *Zbirka izpitnih nalog iz analize*. Ljubljana: DMFA, 1996.

D. Benkovic: *Analiza II* (dodatna gradiva na spletu)

**Cilji in kompetence:**

- Poglobiti znanje glavnih dejstev o krivuljah.
- Poglobiti znanje o ravninskih krivuljah.
- Poglobiti znanje o konstrukcijah krivulj in njihovem zgodovinskem razvoju.

**Objectives and competences:**

- Deepening the knowledge of basic facts about curves.
- Deepening the knowledge of planar curves.
- Deepening the knowledge of constructions of curves and their historical development.

**Predvideni študijski rezultati:**

- Znanje in razumevanje:
- Študent poglobi znanje o osnovah diferencialne geometrije krivulj v ravnini.
  - Študent poglobi znanje o ravninskih krivuljah, njihovih lastnostih in konstrukcijah.

**Intended learning outcomes:**

- Knowledge and Understanding:
- Deepening the knowledge of the basic facts about differential geometry of curves in plane.
  - Deepening the knowledge of the concepts of planar curves, their properties and constructions.

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| <p>Prenesljive/ključne spretnosti in drugi atributi:</p> <ul style="list-style-type: none"> <li>• Prenos znanja v zvezi s krivuljami na druga področja (geografija, astronomija, fizika)</li> </ul> | <p>Transferable/Key Skills and other attributes:</p> <ul style="list-style-type: none"> <li>• Knowledge transfer of the concepts, connected with curves into other fields (geography, astronomy, physics).</li> </ul> |
|---|---|

**Metode poučevanja in učenja:**

**Learning and teaching methods:**

|   |   |
|---|---|
| <ul style="list-style-type: none"> <li>• Predavanja</li> <li>• Seminarji</li> <li>• Seminarske vaje</li> <li>• Individualno delo</li> </ul> | <ul style="list-style-type: none"> <li>• Lectures</li> <li>• Seminars</li> <li>• Tutorial</li> <li>• Individual work</li> </ul> |
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Delež (v %) /

**Načini ocenjevanja:**

**Weight (in %)**

**Assessment:**

|   |     |  |
|---|-----|--|
| Pisni izpit – praktični del   | 40% | Written exam – practical part  |
| Ustni izpit – teoretični del  | 40% | Oral exam – theoretical part   |
| Seminarska naloga   | 20% | Seminar  |
| Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno. |     | Each of the mentioned commitments must be assessed with a passing grade. |
| Pozitivna ocena pri pisnem izpitu je pogoj za pristop k ustnemu izpitu. |     | Passing grade of the written exam is required for taking the oral exam.  |

**Reference nosilca / Lecturer's references:**

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|---|
| <ol style="list-style-type: none"> <li>1. BANIČ, Iztok, ČREPNIJAK, Matevž, MERHAR, Matej, MILUTINOVIĆ, Uroš, SOVIČ, Tina. The closed subset theorem for inverse limits with upper semicontinuous bonding functions. <i>Bulletin of the Malaysian Mathematical Society</i>, ISSN 0126-6705, 2019, vol. 42, iss. 3, str. 835-846, doi: 10.1007/s40840-017-0517-5. [COBISS.SI-ID 23281928].</li> <li>2. BANIČ, Iztok, ČREPNIJAK, Matevž. Inverse component cropping sequences and connected inverse limits over intervals. <i>Glasnik matematički. Serija 3</i>, ISSN 0017-095X, 2018, vol. 53, no. 2, str. 371-384. <a href="https://web.math.pmf.unizg.hr/glasnik/53.2/53(2)-09.pdf">https://web.math.pmf.unizg.hr/glasnik/53.2/53(2)-09.pdf</a>, doi: 10.3336/gm.53.2.09. [COBISS.SI-ID 24323848].</li> <li>3. BANIČ, Iztok, ČREPNIJAK, Matevž. Markov pairs, quasi Markov functions and inverse limits. <i>Houston journal of mathematics</i>, ISSN 0362-1588, 2018, vol. 44, no. 2, str. 695-707. <a href="https://www.math.uh.edu/~hjm/restricted/pdf44(2)/16banic.pdf">https://www.math.uh.edu/~hjm/restricted/pdf44(2)/16banic.pdf</a>. [COBISS.SI-ID 18407001].</li> <li>4. BANIČ, Iztok, ČREPNIJAK, Matevž, MERHAR, Matej, MILUTINOVIĆ, Uroš. The (weak) full projection property for inverse limits with upper semicontinuous bonding functions. <i>Mediterranean journal of mathematics</i>, ISSN 1660-5446, Aug. 2018, vol. 15, iss. 4, str. 1-21, doi: 10.1007/s00009-018-1209-6. [COBISS.SI-ID 23960328].</li> <li>5. ČREPNIJAK, Matevž, TRATNIK, Niko. The Szeged index and the Wiener index of partial cubes with applications to chemical graphs. <i>Applied mathematics and computation</i>, ISSN 0096-3003. [Print ed.], 2017, vol. 309, str. 324-333, doi: 10.1016/j.amc.2017.04.011. [COBISS.SI-ID 23105544].</li> </ol> |
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