



Univerza v Mariboru

Fakulteta za naravoslovje
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Fraktali
Course title:	Fractals

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester
Enovit magistrski študijski program druge stopnje Predmetni učitelj	/	3. ali / or	6. ali / or
Five-year master's degree program Subject Teacher	/	4.	8.

Vrsta predmeta / Course type

Izbirni / Elective

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
30	-	15	-	-	45	3

Nosilec predmeta / Lecturer:

Mateja Grašič

Jeziki /

Predavanja / Lectures:

slovenski / Slovene

Languages:

Vaje / Tutorial:

slovenski / Slovene

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Prerequisites:

/

/

Vsebina:

Content (Syllabus outline):

- Metrični prostor, različne vrste podprostorov, prostor fraktalov.
- Afine transformacije, skrčitve, sistemi iterirajočih funkcij.
- Teoretično in eksperimentalno določanje dimenzije fraktala, Hausdorff-Bezikovičeva dimenzija.

- A metric space, different types of subspaces, the space of fractals.
- Affine transformations, contraction mappings, systems of iterating functions.
- The theoretical and experimental determination of the fractal dimension, Hausdorff-Besicovitch dimension.

Temeljni literatura in viri / Readings:

K. J. Falconer: Fractal Geometry. J. Wiley, Chichester (1990)

Y. Pesin, V. Climenhaga: Elements of Fractal Geometry and Dynamics, spletni vir:
<https://www.math.uh.edu/~climenna/doc/fractals.pdf>

Y. Pesin, V. Climenhaga: Lectures on Fractal Geometry and Dynamical Systems, American Mathematical Society (2009)

J. Vrabc: Metrični prostori. Ljubljana: DMFA (1993).

H. Zeitler, D. Pagon: Fraktale Geometrie: eine Einführung, Vieweg, Braunschweig (2000)

Cilji in kompetence:

Študenti se seznanijo s strukturo podprostora fraktalov v metričnem prostoru in z osnovnimi načini generiranja fraktalov (družine iterirajočih preslikav). Spoznajo tudi nekaj glavnih definicij dimenzije fraktala.

Objectives and competences:

Students get familiar with the structure of the subset of fractals in a metric space and with the main ways of generating fractals (iterated functions systems). They also learn the main definitions of the dimension of a fractal set.

Predvideni študijski rezultati:

Znanje in razumevanje:

- aktivno obvladanje strukture metričnega prostora in prepoznavanje fraktalnih podmnožic
- sposobnost generiranja fraktalov
- teoretično in eksperimentalno določanje dimenzije fraktalov

Intended learning outcomes:

Knowledge and understanding:

- active knowledge of metric space structure and the ability to recognize its fractal subsets
- the ability to generate fractals
- theoretical and experimental ways to find the dimension of a fractal

Metode poučevanja in učenja:

Learning and teaching methods:

<ul style="list-style-type: none"> • Predavanja • Seminarske vaje • Individualno delo 	<ul style="list-style-type: none"> • Lectures • Excercises • Individual work
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Delež (v %) /

Načini ocenjevanja:

Weight (in %)

Assessment:

<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt):</p> <ul style="list-style-type: none"> • pisni izpit – praktični del • ustni izpit – teoretični del <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p> <p>Pozitivna ocena pri pisnem testu je pogoj za pristop k ustnem izpitu.</p>	<p>50%</p> <p>50%</p>	<p>Type (examination, oral, coursework, project):</p> <ul style="list-style-type: none"> • written exam – practical part • oral exam – theoretical part <p>Each of the mentioned commitments must be assessed with a passing grade.</p> <p>Passing grade of the written test is required for taking the oral exam.</p>
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Reference nosilca / Lecturer's references:

1. XIA, Yong-Hui, GRAŠIČ, Mateja, HUANG, Wentao, ROMANOVSKI, Valery. Limit cycles in a model of olfactory sensory neurons. *International journal of bifurcation and chaos in applied sciences and engineering*. 2019, vol. 29, no. 3, str. 1950038-1-1950038-9. ISSN 0218-1274. DOI: [10.1142/S021812741950038X](https://doi.org/10.1142/S021812741950038X). [COBISS.SI-ID [22250006](#)]
2. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Generalized skew derivations on triangular algebras determined by action on zero products. *Communications in algebra*. 2018, vol. 46, iss. 5, str. 1859-1867. ISSN 0092-7872. <https://doi.org/10.1080/00927872.2017.1360334>, DOI: [10.1080/00927872.2017.1360334](https://doi.org/10.1080/00927872.2017.1360334). [COBISS.SI-ID [18505817](#)]
3. GRAŠIČ, Mateja. Zero product determined Jordan algebras, II. *Algebra colloquium*. 2015, vol. 22, iss. 1, str. 109-118. ISSN 1005-3867. DOI: [10.1142/S1005386715000103](https://doi.org/10.1142/S1005386715000103). [COBISS.SI-ID [21136136](#)]
4. BENKOVIČ, Dominik, GRAŠIČ, Mateja. Generalized derivations on unital algebras determined by action on zero products. *Linear Algebra and its Applications*. [Print ed.]. 2014, vol. 445, str. 347-368. ISSN 0024-3795. <http://dx.doi.org/10.1016/j.laa.2013.12.010>. [COBISS.SI-ID [20314120](#)]
5. BIERWIRTH, Hannes, BREŠAR, Matej, GRAŠIČ, Mateja. On maps determined by zero products. *Communications in algebra*. 2012, vol. 40, no. 6, str. 2081-2090. ISSN 0092-7872. <http://dx.doi.org/10.1080/00927872.2011.570833>. [COBISS.SI-ID [16315481](#)]