



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

### UČNI NAČRT PREDMETA / COURSE SYLLABUS

**Predmet:** Nelinearni dinamični sistemi  
**Course title:** Nonlinear Dynamical Systems

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester
Enovit magistrski študijski program druge stopnje Predmetni učitelj Five-year master's degree program Subject Teacher	/	4	8

**Vrsta predmeta / Course type**

izbirni / elective

**Univerzitetna koda predmeta / University course code:**

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
15		30			105	5

**Nosilec predmeta / Lecturer:**

Marko Marhl

**Jeziki /**

**Predavanja / Lectures:** slovenski/Slovenian in/and angleški/English

**Languages:**

**Vaje / Tutorial:** slovenski/Slovenian in/and angleški/English

**Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:**

Predznanje modelske fizike in fizike kompleksnih sistemov

**Prerequisites:**

Preknowledge of physics of complex systems and physics modelling

**Vsebina:**

**Content (Syllabus outline):**

<p><b>1. Nelinearni dinamični sistemi v 1D, 2D in 3D</b></p> <p>Linearizacija in linearna stabilnostna analiza, bifurkacijska analiza, nelinearni oscilatorji.</p>
<p><b>2. Kvaziperiodičnost, kaotični in čudni atraktorji</b></p> <p>Fourierjeva transformacija in avtokorelacija, Lyapunovi eksponenti, kaos, fraktali in fraktalne dimenzije.</p>
<p><b>3. Stohastično modeliranje (Gillespiev algoritem)</b></p>
<p><b>4. Aplikacije</b></p> <p>Pomen dinamičnih sistemov v fiziki in na drugih področjih: dinamični sistemi v biologiji, okoljevarstvu, ekonomiji, ....</p>
<p><b>5. Uporaba računalniških programov</b></p> <p>Uporaba računalniških programov za implementacijo dinamičnih sistemov: DynaSys, Stella, Madonna, C++, ...</p>

<p><b>1. Nonlinear dynamical systems (1D-, 2D-, 3D-systems)</b></p> <p>Linearization and the linear stability analysis, the bifurcation analysis, non-linear oscillators.</p>
<p><b>2. Quasiperiodicity, chaotic and strange attractors</b></p> <p>Fourier transformation and autocorrelation, Lyapunov exponents, chaos, fractals and fractal dimensions.</p>
<p><b>3. Stochastic modelling (Gillespie's algorithm)</b></p>
<p><b>4. Applications</b></p> <p>The role of dynamical systems in physics and in other fields: dynamical systems in biology, environmental science, economy, ...</p>
<p><b>5. Using of computer programs</b></p> <p>Computer programmes for the implementation of dynamical systems: DynaSys, Stella, Madonna, C++, ...</p>

**Temeljni literatura in viri / Readings:**

<ol style="list-style-type: none"> <li>1. Steven H. Strogatz, Nonlinear Dynamics and Chaos with Applications to Physics, Biology, Chemistry, and Engineering. Perseus Pub., Cambridge, 1994.</li> <li>2. J. B. Snape, I. J. Dunn, J. Ingham, J. E. Prenosil, Dynamics of Environmental Bioprocesses, Modelling and Simulation, VCH Verlagsgesellschaft, Weinheim, 1995.</li> <li>3. Natali Hritonenko, Yuri Yatsenko, Mathematical Modeling in Economics, Ecology and the Environment, Springer, New York, 1999.</li> <li>4. Strokovni in znanstveni članki v revijah / Articles published in professional and scientific journals.</li> </ol>
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**Cilji in kompetence:**

**Objectives and competences:**

- Razvijati sposobnosti za opravljanje kvantitativne analize dinamike kompleksnih sistemov.
- Predstaviti ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Poudariti uporabnost znanja o dinamičnih sistemih v naravnih sistemih in prenos znanja na druga področja.
- Uporaba računalniških programov za implementacijo dinamičnih sistemov.

- Developing skills for quantitative analysis of the dynamics of complex systems.
- Presenting basic differences and characteristics of dynamical systems in different dimensions.
- Pointing out the applicability of knowledge about dynamical systems in the nature and the transfer of knowledge to other fields.
- Using computer programs for the implementation of dynamical systems.

**Predvideni študijski rezultati:**

- Znanje in razumevanje:
- Usvojiti metode za kvantitativno analizo dinamike kompleksnih sistemov.
  - Spoznati ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
  - Pomen determinističnega in stohastičnega modeliranja.
  - Spoznati uporabnost znanja o dinamičnih sistemih v fiziki in prenos znanja na druga področja.
  - Znati uporabljati računalniške programe za implementacijo dinamičnih sistemov.
- Prenesljive/ključne spretnosti in drugi atributi:
- Metode kvantitativne analize dinamičnih sistemov so univerzalne in jih je mogoče uporabiti na najrazličnejših področjih.
  - Poudarek je na prenosu znanja s primerov iz fizike na področja biologije, ekologije, ekonomije, ...

**Intended learning outcomes:**

- Knowledge and Understanding:
- Be able to use methods for quantitative analysis of the dynamics of complex systems.
  - Know basic differences and characteristics of dynamical systems in different dimensions.
  - Importance of deterministic and stochastic modelling.
  - Be able to apply the knowledge about dynamical systems in physics to other fields.
  - Using computer programs for the implementation of dynamical systems.
- Transferable/Key Skills and other attributes:
- Methods for quantitative analysis of dynamical system are universal and can be implemented in different fields of research.
  - In particular, a knowledge transfer from examples in physics to examples in biology, ecology, economics, etc. is emphasised.

**Metode poučevanja in učenja:**

- Predavanja
- Teoretične vaje
- Vaje na računalniku
- Eksperimentalne vaje

**Learning and teaching methods:**

- Lectures
- Theoretical exercises
- Computer exercises
- Experiments

**Načini ocenjevanja:**

Delež (v %) /

**Assessment:**

Weight (in %)

<ul style="list-style-type: none"> <li>• ustno</li> <li>• pisno</li> <li>• praktično - seminar</li> </ul>	<p>40</p> <p>40</p> <p>20</p>	<ul style="list-style-type: none"> <li>• oral</li> <li>• written</li> <li>• practical - seminar</li> </ul>
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**Reference nosilca / Lecturer's references:**

BODENSTEIN, Christian, KNOKE, Beate, MARHL, Marko, PERC, Matjaž, SCHUSTER, Stefan. Using Jensen's inequality to explain the role of regular calcium oscillations in protein activation. *Physical biology*, 2010, vol. 7, no. 3, str. 036009-1-036009-12, doi: [10.1088/1478-3975/7/3/036009](https://doi.org/10.1088/1478-3975/7/3/036009). [COBISS.SI-ID [14376470](#)]

GOSAK, Marko, KOROŠAK, Dean, MARHL, Marko. Optimal network configuration for maximal coherence resonance in excitable systems. *Phys. rev., E Stat. nonlinear soft matter phys. (Print)*, 2010, vol. 81, iss. 5, str. 056104-1-056104-7, ilustr., doi: [10.1103/PhysRevE.81.056104](https://doi.org/10.1103/PhysRevE.81.056104). [COBISS.SI-ID [17626120](#)]

KNOKE, Beate, BODENSTEIN, Christian, MARHL, Marko, PERC, Matjaž, SCHUSTER, Stefan. Jensen's inequality as a tool for explaining the effect of oscillations on the average cytosolic calcium concentration. *Theory biosci.*, Jun. 2010, vol. 129, no. 1, str. 25-38, doi: [10.1007/s12064-010-0080-1](https://doi.org/10.1007/s12064-010-0080-1). [COBISS.SI-ID [14376726](#)]

GOSAK, Marko, KOROŠAK, Dean, MARHL, Marko. Topologically determined optimal stochastic resonance responses of spatially embedded networks. *New journal of physics*. [Online ed.], Jan. 2011, vol. 13, issue 1, str. 013012-1-013012-15, ilustr. <http://dx.doi.org/10.1088/1367-2630/13/1/013012>. [COBISS.SI-ID [18087432](#)]

GOSAK, Marko, MARKOVIČ, Rene, MARHL, Marko. The role of neural architecture and the speed of signal propagation in the process of synchronization of bursting neurons. *Physica, A*. [Print ed.], 2012, vol. 391, no. 8, str. 2764-2770, ilustr., doi: [10.1016/j.physa.2011.12.027](https://doi.org/10.1016/j.physa.2011.12.027). [COBISS.SI-ID [18948872](#)]