



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS							
<b>Predmet:</b>	<b>Geometrija</b>						
<b>Course title:</b>	Geometry						
<b>Študijski program in stopnja</b> Study programme and level	<b>Študijska smer</b> Study field			<b>Letnik</b> Academic year	<b>Semester</b> Semester		
Matematika				3.	6.		
Mathematics				3.	6.		
<b>Vrsta predmeta / Course type</b>							
<b>Univerzitetna koda predmeta / University course code:</b>							
<b>Predavanja</b> Lectures	<b>Seminar</b> Seminar	<b>Sem. vaje</b> Tutorial	<b>Lab. vaje</b> Laboratory work	<b>Teren. vaje</b> Field work	<b>Samost. delo</b> Individ. work		<b>ECTS</b>
45		30			105		6
<b>Nosilec predmeta / Lecturer:</b> Tanja Dravec							
<b>Jeziki /</b> Languages:	<b>Predavanja /</b> Lectures:		SLOVENSKO/SLOVENE				
	<b>Vaje / Tutorial:</b>		SLOVENSKO/SLOVENE				
<b>Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:</b>				<b>Prerequisites:</b>			
Vsaka izmed naštetih obveznosti v načinih ocenjevanja mora biti opravljena s pozitivno oceno.  Pozitivna ocena pri pisnem izpitu je pogoj za pristop k ustnemu izpitu.				Each of the mentioned commitments must be assessed with a passing grade.  Passing grade of the written exam is required for taking the oral exam.			
<b>Vsebina:</b>				<b>Content (Syllabus outline):</b>			
Hilbertov aksiomatski sistem za absolutno geometrijo: aksiomi povezave, urejenosti, skladnosti in zveznosti. Aksiom o vzporednicah in njegovi ekvivalenti.				Hilbert's axiomatic system for absolute geometry: incidence axioms, ordering axioms, congruence axioms and continuity axioms. Parallel postulate and its equivalents. .			

<p>Afini prostori, affine transformacije, aksiomatsko definirana afina geometrija.</p> <p>Aksiomi projektivne geometrije, Desarguesov izrek. Harmonični elementi. Homogene in nehomogene koordinate v projektivni ravnini. Projektivne transformacije.</p>	<p>Affine spaces, affine transformations, axiomatic definition of affine geometry.</p> <p>Axioms of projective geometry, Desargues' theorem. Harmonic elements. Homogeneous and non-homogeneous coordinate systems in the projective plane. Projective transformations.</p>
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### Temeljni literatura in viri / Readings:

1. Coxeter, H. S. M. (1993). *The real projective plane: with an appendix for mathematica by George Beck: PC Version (Diskette provided)* (3rd ed., str. XIII, 222). Springer.
2. Mitrović, M. (2009). *Projektivna geometrija* (Let. 88, str. 150). DMFA - založništvo.
3. Vidav, I. (1981). *Afina in projektivna geometrija* (Let. 15, str. 170). Društvo matematikov, fizikov in astronomov SRS.
4. Rosenbaum, R. A. (1963). *Introduction to projective geometry and modern algebra* (str. VIII, 344). Addison-Wesley.
5. Pagon, D. (1995). *Osnove evklidske geometrije* (str. 124). DZS.
6. Berger, M. (1987). *Geometry I: with 426 figures* (str. XIII, 427). Springer.

### Dodatna literatura / Additional Readings:

1. Ayres, F. (1967). *Schaum's outline of theory and problems of projective geometry* (str. 243). McGraw-Hill.

### Cilji in kompetence:

Študentje spoznajo aksiomatsko zasnovo evklidske geometrije ter osnove affine in projektivne geometrije.

### Objectives and competences:

Students get familiar with axiomatic approach to Euclidean geometry and the basic concepts of affine and projective geometry.

### Predvideni študijski rezultati:

Znanje in razumevanje:  
Po zaključku tega predmeta bo študent sposoben

- razumevati Hilbertov aksiomatski sistem za evklidsko geometrijo.
- razložiti in uporabljati osnovne izreke evklidske geometrije.
- poznati osnovne pojme affine in projektivne geometrije.

### Intended learning outcomes:

Knowledge and Understanding:  
On completion of this course the student will be able to

- understand the Hilbert axiomatic system for Euclidean geometry.
- explain and use basic theorems from Euclidean geometry.
- recognize the basic concepts of affine

<ul style="list-style-type: none"> <li>• razlikovati med različnimi neevklidskimi geometrijami.</li> </ul> <p>Prenesljive/ključne spretnosti in drugi atributi:</p> <ul style="list-style-type: none"> <li>• Pridobljena znanja prispevajo k razumevanju ostalih predmetov s področja geometrije in topologije.</li> </ul>	<p>and projective geometry</p> <ul style="list-style-type: none"> <li>• distinguish between different non-Euclidean geometries.</li> </ul> <p>Transferable/Key Skills and other attributes:</p> <ul style="list-style-type: none"> <li>• The obtained knowledge contributes to better understanding of other subjects in fields of geometry and topology.</li> </ul>
<p><b>Metode poučevanja in učenja:</b></p> <ul style="list-style-type: none"> <li>• Predavanja</li> <li>• Teoretične vaje</li> </ul>	<p><b>Learning and teaching methods:</b></p> <ul style="list-style-type: none"> <li>• Lectures</li> <li>• Theoretical exercises</li> </ul>

Načini ocenjevanja	Delež (v %)/ Weight (in %)	Assessment:
Pisni izpit	50%	Written exam
Ustni izpit	50%	Oral exam

**Opombe:**

Pisni izpit se lahko nadomesti s kolokviji v enakem deležu 50%.

**Comments:**

Written exam can be replaced by written midterm examination in the weight of 50%.

**Reference nosilca / Lecturer's references:**

1. BREŠAR, Boštjan, DRAVEC, Tanja, KLESZCZ, Elżbieta. Uniquely colorable graphs up to automorphisms. *Applied mathematics and computation*. [Print ed.]. Aug. 2023, vol. 450, art. 128007 (10 str.). ISSN 0096-3003. <https://www.sciencedirect.com/science/article/pii/S0096300323001765>, DOI: [10.1016/j.amc.2023.128007](https://doi.org/10.1016/j.amc.2023.128007).
2. DRAVEC, Tanja, TARANENKO, Andrej. Daisy Hamming graphs. *Discussiones mathematicae. Graph theory*. 2023, vol. 43, no. 2, str. 421-436. ISSN 1234-3099. DOI: [10.7151/dmgt.2373](https://doi.org/10.7151/dmgt.2373).
3. DRAVEC, Tanja, JAKOVAC, Marko, KOS, Tim, MARC, Tilen. On graphs with equal total domination and Grundy total domination numbers. *Aequationes mathematicae*. Feb. 2022, vol. 96, iss. 1, 137-146. ISSN 0001-9054. <https://link.springer.com/article/10.1007/s00010-021-00776-z>, DOI: [10.1007/s00010-021-00776-z](https://doi.org/10.1007/s00010-021-00776-z).
4. BREŠAR, Boštjan, DRAVEC, Tanja, GORZKOWSKA, Aleksandra, KLESZCZ, Elżbieta. Graphs with a unique maximum independent set up to automorphisms. *Discrete applied mathematics*. [Print ed.]. Aug. 2022, vol. 317, str. 124-135. ISSN 0166-218X. <https://www.sciencedirect.com/science/article/pii/S0166218X22001251>,

DOI: [10.1016/j.dam.2022.04.003](https://doi.org/10.1016/j.dam.2022.04.003).

5. DRAVEC, Tanja. On the toll number of a graph. *Discrete applied mathematics*. [Print ed.]. Nov. 2022, vol. 321, str. 250-257. ISSN 0166-218X. DOI: [10.1016/j.dam.2022.07.006](https://doi.org/10.1016/j.dam.2022.07.006).