



Univerza v Mariboru

Fakulteta za naravoslovje
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Linearna algebra
Course title:	Linear Algebra

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Matematika		1.	2.
Mathematics		1.	2.

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
60		60			120	8

Nosilec predmeta / Lecturer:

Daniel Eremita

Jeziki /

Languages:

Predavanja /

Lectures:

SLOVENSKO/SLOVENE

Vaje / Tutorial:

SLOVENSKO/SLOVENE

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Jih ni.

Prerequisites:

There are none.

Vsebina:

Vektorski prostori: prostori in podprostori; baza; dimenzija; vsote in direktne vsote.

Linearne preslikave: primeri in osnovne lastnosti; jedro in slika; prostori linearnih preslikav; izomorfizmi vektorskih prostorov.

Linearne preslikave in matrike: matriki prirejena preslikava; preslikavi prirejena matrika; sprememba baze in podobne matrike.

Lastne vrednosti in lastni vektorji: osnovne lastnosti; zgornje trikotne matrike; minimalni

Content (Syllabus outline):

Vector spaces: spaces and subspaces; base; dimension; sums and direct sums.

Linear transformations: examples and basic properties; kernel and image; spaces of linear transformations; isomorphisms.

Linear transformations and matrices: transformation of a matrix; matrix of a transformation; base change and similar matrices.

polinom; karakteristični polinom; Cayley-Hamiltonov izrek; diagonalizacija; Jordanova kanonična forma.

Prostori s skalarnim produktom: Evklidski prostori; unitarni prostori; pravokotnost in ortogonalne baze; ortogonalni komplementi; dualni prostor in Rieszov izrek.

Preslikave v Evklidskih in unitarnih prostorih: adjungirane; normalne; sebi-adjungirane; ortogonalne in unitarne; pozitivno (semi)definitne.

Eigenvalues and eigenvectors: basic properties; upper triangular matrices; minimal polynomial; characteristic polynomial; Cayley-Hamilton theorem; diagonalization; Jordan canonical form.

Spaces with inner product: Euclidean spaces; unitary spaces; orthogonality and orthogonal bases; orthogonal complement; dual spaces and Riesz theorem.

Transformations in Euclidean and unitary spaces: adjoint; normal; self-adjoint; orthogonal and unitary; positive (semi)definite.

Temeljni literatura in viri / Readings:

T. Košir, Linearna algebra (spletna skripta)
<http://www.fmf.unilj.si/~kosir/poucevanje/0607/linalg.html>
<http://www.fmf.uni-lj.si/~kosir/poucevanje/0809/alg1-fm.html>
 M. Kolar, B. Zgrablič, Več kot nobena, a manj kot tisoč in ena rešena naloga iz linearne algebre, Pedagoška fakulteta Ljubljana, Ljubljana, 1996.
 C. Scheiderer, Lineare Algebra I und II (spletna skripta)
<http://www.uni-duisburg.de/FB11/LEHRE/LINALG/LA.public.pdf>
 M. Dobovišek, D. Kobal, B. Magajna, Naloge iz algebre I, DMFA založništvo, Ljubljana, 2005.
 R. Kaye, R. Wilson, Linear Algebra, Oxford University Press, Oxford, 1998.

Cilji in kompetence:

Temeljito spoznati vektorske prostore in linearne preslikave.

Objectives and competences:

To know thoroughly vector spaces and linear transformation.

Predvideni študijski rezultati:

Znanje in razumevanje:

- Razumevanje vektorskih prostorov in linearnih transformacij.
- Povezovanje teorije s predmetov »Vektorji in matrike«.

Prenosljive/ključne spretnosti in drugi atributi:

- Pridobljena znanja so podlaga za večino predmetov v nadaljevanju študija.

Intended learning outcomes:

Knowledge and Understanding:

- Be able to understand vector spaces and linear transformations.
- Be able to connect the theory with the subject »Vectors and Matrices«.

Transferable/Key Skills and other attributes:

- The obtained knowledge is a basis for most of the later subjects.

Metode poučevanja in učenja:

Learning and teaching methods:

<ul style="list-style-type: none"> • Predavanja • Teoretične vaje 	<ul style="list-style-type: none"> • Lectures • Theoretical exercises 	
Načini ocenjevanja:	Assessment:	
<p><u>Izpit:</u></p> <p>Pisni izpit – problemi, Ustni izpit – teorija.</p> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p> <p>Opravljen pisni izpit – problemi je pogoj za pristop k ustnemu izpitu – teorija.</p> <p>Pisni izpit – problemi se lahko nadomesti z dvema delnima testoma (sprotne obveznosti).</p>	<p>Delež (v %) / Weight (in %)</p> <p>50% 50%</p>	<p><u>Exams:</u></p> <p>Written exam – problems, Oral exam – theory.</p> <p>Each of the mentioned assessments must be assessed with a passing grade.</p> <p>Passing grade of written exam – problems is required to take the oral exam – theory.</p> <p>Written exam – problems can be repalced with two mid-term tests.</p>

Reference nosilca / Lecturer's references:

1. EREMITA, Daniel. Biderivations on tensor products of algebras. *Communications in algebra*, ISSN 0092-7872, 2018, vol. 46, iss. 4, str. 1722-1726. <http://doi.org/10.1080/00927872.2017.1355375>, doi: [10.1080/00927872.2017.1355375](https://doi.org/10.1080/00927872.2017.1355375).
2. EREMITA, Daniel. Commuting traces of upper triangular matrix rings. *Aequationes mathematicae*, ISSN 0001-9054, June 2017, vol. 91, iss. 3, str. 563-578. <http://doi.org/10.1007/s00010-016-0462-7>, doi: [10.1007/s00010-016-0462-7](https://doi.org/10.1007/s00010-016-0462-7).
3. EREMITA, Daniel. Biderivations of triangular rings revisited. *Bulletin of the Malaysian Mathematical Society*, ISSN 0126-6705, Apr. 2017, vol. 40, iss. 2, str. 505-522. <http://doi.org/10.1007/s40840-017-0451-6>, doi: [10.1007/s40840-017-0451-6](https://doi.org/10.1007/s40840-017-0451-6).
4. EREMITA, Daniel. Functional identities in upper triangular matrix rings. *Linear Algebra and its Applications*, ISSN 0024-3795. [Print ed.], 2016, vol. 493, str. 580-605. <http://dx.doi.org/10.1016/j.laa.2015.12.022>.
5. EREMITA, Daniel. Functional identities of degree 2 in triangular rings revisited. *Linear and Multilinear Algebra*, ISSN 0308-1087, 2015, vol. 63, iss. 3, str. 534-553. <http://dx.doi.org/10.1080/03081087.2013.877012>.