Univerza v Mariboru

Fakulteta za naravoslovje in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS	
Predmet:	**Teorija števil**
Course title:	Number Theory

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Matematika		**3.**	**6.**
Mathematics		**3.**	**6.**

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
45		**45**			**150**	**8**

Nosilec predmeta / Lecturer: Daniel EREMITA

Jeziki / Languages:	**Predavanja / Lectures:**	SLOVENSKO/SLOVENE
	Vaje / Tutorial:	SLOVENSKO/SLOVENE

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	**Prerequisits:**
Jih ni.	There are none.

Vsebina:	**Content (Syllabus outline):**
Deljivost celih števil. Največji skupni delitelj. Evklidov algoritem. Najmanjši skupni večkratnik. Linearne diofantske enačbe. Praštevila. Osnovni izrek aritmetike. Kongruence. Kriteriji deljivosti. Linearne kongruence. Kitajski izrek o ostankih. Reševanje polinomskih kongruenc. Wilsonov izrek. Fermatov mali izrek in psevdopraštevila. Eulerjev izrek. Aritmetične funkcije. Multiplikativne funkcije. Möbiusova formula inverzije.	Divisibility of integers. Greatest common divisor. Euclidean algorithm. Least common multiple. Linear Diophantine equations. Primes. Fundamental Theorem of Arithmetic. Congruences. Special divisibility tests. Linear congruences. Chinese Remainder Theorem. Solving polynomial congruences. Wilson's Theorem. Fermat's Little Theorem and pseudoprimes. Euler's Theorem. Arithmetic functions. Multiplicative functions. Möbius inversion.

Red celega števila in primitivni koreni. Kvadratični zakon recipročnosti. Pitagorejske trojke.	The Order of an Integer and Primitive roots. The law of quadratic reciprocity. Pythagorean Triples.

Temeljni literatura in viri / Readings:

D. M. Burton: Elementary Number Theory. New York [etc.] : McGraw-Hill, 1998.
K. H. Rosen: Elementary number theory and its applications. Boston: Pearson/Addison Wesley, cop. 2005.
J. Grasselli: Elementarna teorija števil. Ljubljana: DMFA, 2009.
J. Grasselli: Diofantske enačbe. Ljubljana: DMFA, 1984.
J. Grasselli: Osnove teorije števil. Ljubljana: DMFA, 1975.

Cilji in kompetence:	**Objectives and competences:**
Proučiti temeljne koncepte in rezultate elementarne teorije števil.	To study the fundamental concepts and results of elementary number theory.

Predvideni študijski rezultati:	**Intended learning outcomes:**
Znanje in razumevanje pojmov in rezultatov elementarne teorije števil. Prenesljive/ključne spretnosti in drugi atributi: • Pridobljena znanja se dopolnjujejo z znanji s podrocja algebre, kombinatorike, kriptografije, teorije kodiranja, analize, računalništva, …	Knowledge and Understanding of notions and results of elementary number theory. Transferable/Key Skills and other attributes: • The obtained knowledge supplements with the knowledge of algebra, combinatorics, cryptography, coding theory, analysis, computer science, …

Metode poučevanja in učenja:	**Learning and teaching methods:**
• Predavanja • Teoretične vaje	• Lectures • Theoretical exercises

Načini ocenjevanja:		**Assessment:**
Izpit: Pisni izpit – problemi, Ustni izpit – teorija. Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno. Opravljen pisni izpit – problemi je pogoj za pristop k ustnemu izpitu – Teorija. Pisni izpit – problemi se lahko nadomesti z dvema delnima testoma (sprotne obveznosti).	Delež (v %) / Weight (in %) 50% 50%	Exams: Written exam – problems, Oral exam – theory. Each of the mentioned assessments must be assessed with a passing grade. Passing grade of written exam – problems is required to take the oral exam – theory. Written exam – problems can be repalced with two mid-term tests.

Reference nosilca / Lecturer's references:		

1. EREMITA, Daniel. Functional identities in upper triangular matrix rings. Linear Algebra and its Applications, ISSN 0024-3795. [Print ed.], 2016, vol. 493, str. 580-605. http://dx.doi.org/10.1016/j.laa.2015.12.022.

2. EREMITA, Daniel. Functional identities of degree 2 in triangular rings revisited. Linear and Multilinear Algebra, ISSN 0308-1087, 2015, vol. 63, iss. 3, str. 534-553. http://dx.doi.org/10.1080/03081087.2013.877012.

3. EREMITA, Daniel, GOGIĆ, Ilja, ILIŠEVIĆ, Dijana. Generalized skew derivations implemented by elementary operators. Algebras and representation theory, ISSN 1386-923X, 2014, vol. 17, iss. 3, str. 983-996. http://dx.doi.org/10.1007/s10468-013-9429-8.

4. EREMITA, Daniel. Functional identities of degree 2 in triangular rings. Linear Algebra and its Applications, ISSN 0024-3795. [Print ed.], 2013, vol. 438, iss 1, str. 584-597. http://dx.doi.org/10.1016/j.laa.2012.07.028.

5. EREMITA, Daniel, ILIŠEVIĆ, Dijana. On (anti-)multiplicative generalized derivations. Glasnik matematički. Serija 3, ISSN 0017-095X, 2012, vol. 47, no. 1, str. 105-118. http://dx.doi.org/10.3336/gm.47.1.08.