

### UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Osnove analize
Course title:	Basic Analysis

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Fizika, 1. stopnja		1.	1.
Physics, 1 <sup>st</sup> degree		1.	1.

Vrsta predmeta / Course type	Obvezni / Mandatory
------------------------------	---------------------

Univerzitetna koda predmeta / University course code:	
---	--

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
60		45			135	8

Nosilec predmeta / Lecturer:	Iztok BANIČ
------------------------------	-------------

Jeziki / Languages:	Predavanja / Lectures: SLOVENSKO/SLOVENIAN
	Vaje / Tutorial: SLOVENSKO/SLOVENIAN

**Pogoji za vključitev v delo oz. za opravljanje  
študijskih obveznosti:**

Priporočeno je predznanje maturitetnega kurza  
matematike.

**Prerequisites:**

Matura-level knowledge of mathematics is  
recommended.

**Vsebina:**

**Content (Syllabus outline):**

<p>1. Funkcije ene realne spremenljivke. Pregled elementarnih funkcij. Zveznost in limita funkcij.</p> <p>2. Definicija in geometrijski pomen odvoda, odvodi elementarnih funkcij, pravila za odvajanje. Analiza poteka funkcije; monotonost, konveksnost in konkavnost; ekstremi in prevoji. Lagrangeov izrek, L'Hospitalovo pravilo. Višji odvodi.</p> <p>3. Zaporedja, vrste, potenčne vrste, Taylorjeve vrste.</p> <p>4. Definicija nedoločenega integrala, metode integriranja, integrali elementarnih funkcij. Definicija določenega integrala. Newton-Leibnizova formula. Uporaba določenega integrala.</p>	<p>1. Functions of one real variable. Elementary functions. Continuity and limits of functions.</p> <p>2. Definition and geometric meaning of a derivative, derivatives of elementary functions, rules for calculating derivatives. Determining the graph of a function; monotonicity, convexity, maxima and minima, inflection points. Mean value theorems. L'Hospital's rule. Higher order derivatives.</p> <p>3. Sequences, series, power series, Taylor's series.</p> <p>4. Indefinite integrals, methods of integration, integrals of elementary functions. Definition of the definite integral. The fundamental theorem of the calculus. Applications.</p>
--	--

#### **Temeljni literatura in viri / Readings:**

1. I. Vidav: Višja matematika I. Ljubljana, DZS, 1974
2. F. Ayres, J., E. Mendelson: Schaum's Outline of Calculus, New York, McGraw-Hill, 1962 (Fourth Edition, 1999)
3. E. Mendelson: 3000 Solved Problems in Calculus. New York, McGraw-Hill, 1988

#### **Cilji in kompetence:**

Študentje obvladajo temeljne pojme in metode analize, na nivoju diferencialnega in integralnega računa funkcij ene realne spremenljivke. Te pojme in metode so sposobni uporabiti pri nadaljnjem študiju fizike.

#### **Objectives and competences:**

Students learn the fundamental concepts and methods of the calculus of functions of one real variable. The students are able to use the concepts and methods latter in the study of physics.

#### **Predvideni študijski rezultati:**

##### **Znanje in razumevanje.**

Po uspešnem zaključku tega predmeta bodo študentje:

1. Obvladali elementarne funkcije in njihove lastnosti.
2. Razumeli pojem limita funkcije in znali računati limite.
3. Razumeli pojem odvoda funkcij in znali računati odvode.
4. Znali uporabiti odvod pri analizi poteka funkcije; obravnavi monotonosti, konveksnosti

#### **Intended learning outcomes:**

##### **Knowledge and understanding.**

After successful conclusion of this course the students will:

1. Know elementary functions and their properties.
2. Understand the concept of the limit of a function and know how to calculate them.
3. Understand the concept of the derivative of a function and know how to calculate them.
4. Know how to use derivatives in determining the graph of a function; in study of monotonicity,

<p>in konkavnosti; določanju ekstremov in prevojev.</p> <p>5. Obvladali Lagrangeov izrek in L'Hospitalovo pravilo.</p> <p>6. Obvladali delo z zaporedji, vrstami, potenčnimi vrstami, Taylorjevimi vrstami.</p> <p>7. Razumeli pojem nedoločenega integrala, obvladali metode integriranja in jih znali uporabiti.</p> <p>8. Razumeli pojem določenega integrala, obvladali Newton-Leibnizovo formulo in njeno uporabo.</p> <p>9. Znali uporabiti določeni integral v različnih situacijah.</p>
<p><b>Prenesljive/ključne spretnosti in drugi atributi:</b> Matematično orodje, ki je nujno potrebno za delo pri vseh fizikalnih predmetih.</p>

<p>convexity, maxima and minima, inflexion points.</p> <p>5. Know how to use mean value theorems and L'Hospital's rule.</p> <p>6. Know how to use sequences, series, power series, Taylor's series.</p> <p>7. Understand the concept of the indefinite integral and know the methods of integration, and how to use them.</p> <p>8. Understand the concept of the definite integrals and know the fundamental theorem of the calculus, and how to use it.</p> <p>9. Know different applications of definite integral.</p>
<p><b>Transferable/Key Skills and other attributes:</b> Knowledge of mathematical tools that is essential for all the subjects on physics</p>

<p><b>Metode poučevanja in učenja:</b></p> <ul style="list-style-type: none"> <li>• Predavanja</li> <li>• Teoretične vaje</li> </ul>
--

<p><b>Learning and teaching methods:</b></p> <ul style="list-style-type: none"> <li>• Lectures</li> <li>• Theoretical exercises</li> </ul>
--

Načini ocenjevanja:	Delež (v %) / Weight (in %)	Type (examination, oral, coursework, project):
<p><u>Izpit:</u></p> <p>Pisni izpit – problemi Ustni izpit – teorija</p> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p> <p>Pozitivna ocena pri pisnem izpitu - problemi je pogoj za pristop k ustnemu izpitu – teorija.</p> <p>Pisni izpit – problemi se lahko nadomesti z dvema delnima testoma (ki sta sprotni obveznosti).</p>	<p>50% 50%</p>	<p><u>Exams:</u></p> <p>Written exam – problems Oral exam – theory</p> <p>Each of the mentioned assessments must be assessed with a passing grade.</p> <p>Passing grade of the written exam – problems is required for taking the oral exam – theory.</p> <p>Written exam – problems can be replaced by two mid-term tests.</p>

## Reference nosilca / Lecturer's references:

1. BANIČ, Iztok, ŽEROVNIK, Janez. On median and quartile sets of ordered random variables. *The art of discrete and applied mathematics*. 2020, vol. 3, no. 2, str. 1-18. ISSN 2590-9770. <https://adam-journal.eu/index.php/ADAM/article/view/1326>, DOI: [10.26493/2590-9770.1326.9fd](https://doi.org/10.26493/2590-9770.1326.9fd). [COBISS.SI-ID [17163291](#)], [[SNIP](#), [Scopus](#)]
2. BANIČ, Iztok, GREENWOOD, Sina. A characterisation of the dimension of inverse limits of set-valued functions on intervals. *Fundamenta mathematicae*. 2020, vol. 249, no. 1, str. 1-19. ISSN 0016-2736. DOI: [10.4064/fm708-5-2019](https://doi.org/10.4064/fm708-5-2019). [COBISS.SI-ID [24853768](#)], [[JCR](#), [SNIP](#), [Scopus](#)] do 1. 3. 2021: št. citatov (TC): 2, čistih citatov (CI): 1, čistih citatov na avtorja (CIAu): 0,50]
3. BANIČ, Iztok, ČREPNJAK, Matevž, GORIČAN, Peter, KAC, Teja, MERHAR, Matej, MILUTINOVIC, Uroš. Big and large continua in inverse limits of inverse systems over directed graphs. *Topology and its Applications*. [Print ed.]. Apr. 2020, vol. 274, str. 1-18. ISSN 0166-8641. DOI: [10.1016/j.topol.2020.107119](https://doi.org/10.1016/j.topol.2020.107119). [COBISS.SI-ID [25211400](#)], [[JCR](#), [SNIP](#), [WoS](#), [Scopus](#)]  
financer: ARRS, Programi, P1-0297, SI, Teorija grafov; ARRS, Programi, P1-0285, SI, Algebra, diskretna matematika, verjetnostni račun in teorija iger; ARRS, Programi, P1-0403, SI, Računsko intenzivni kompleksni sistemi
4. BANIČ, Iztok, ČREPNJAK, Matevž, MERHAR, Matej, MILUTINOVIC, Uroš, SOVIČ, Tina. The closed subset theorem for inverse limits with upper semicontinuous bonding functions. *Bulletin of the Malaysian Mathematical Sciences Society*. 2019, vol. 42, iss. 3, str. 835-846. ISSN 0126-6705. DOI: [10.1007/s40840-017-0517-5](https://doi.org/10.1007/s40840-017-0517-5). [COBISS.SI-ID [23281928](#)], [[JCR](#), [SNIP](#), [WoS](#)] do 9. 8. 2021: št. citatov (TC): 3, čistih citatov (CI): 1, čistih citatov na avtorja (CIAu): 0,20, [[Scopus](#)] do 29. 12. 2020: št. citatov (TC): 3, čistih citatov (CI): 1, čistih citatov na avtorja (CIAu): 0,20]
5. BANIČ, Iztok, GOODWIN, Simon, LOCKYER, Michael. Extending bonding functions in generalized inverse sequences. *Topology and its Applications*. [Print ed.]. March 2019, vol. 254, str. 85-100. ISSN 0166-8641. <https://doi.org/10.1016/j.topol.2018.12.004>, DOI: [10.1016/j.topol.2018.12.004](https://doi.org/10.1016/j.topol.2018.12.004). [COBISS.SI-ID [24333576](#)], [[JCR](#), [SNIP](#), [WoS](#), [Scopus](#)]  
financer: ARRS, Programi, P1-0285 (B), SI, Algebra, diskretna matematika, verjetnostni račun in teorija iger