



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

**UČNI NAČRT PREDMETA / COURSE SYLLABUS**

<b>Predmet:</b>	Izbor iz matematike za ekologe
<b>Course title:</b>	Selection in Mathematics for Ecologists

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Doktorski študij Ekološke znanosti, 3. stopnja		1. ali 2.; 1st or 2nd	1. 2. ali 3. ; 1st, 2nd or 3rd
Doctoral Study Ecological Sciences, 3rd degree			

**Vrsta predmeta / Course type**

**Univerzitetna koda predmeta / University course code:**

Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Lab. vaje Laboratory work	Terenske vaje Field work	Samost. delo Individ. work	ECTS
5		5			140	5

**Nosilec predmeta / Lecturer:**

<b>Jeziki /</b>	<b>Predavanja / Lectures:</b>	slovenski / slovene
<b>Languages:</b>	<b>Vaje / Tutorial:</b>	slovenski / slovene

**Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:**

Poznavanje matematike na ravni dodiplomskega programa

**Prerequisites:**

Knowledge of mathematics at undergraduate level

**Vsebina:**

Obravnavana so izbrana poglavja iz naslednjih sklopov.

- Funkcije več realnih spremenljivk. Definicija in zveznost, parcialni odvod in totalni diferencial, višji parcialni odvodi, ekstremi, Taylorjeva vrsta.
- Diferencialne enačbe. Osnovni pojmi, preproste diferencialne enačbe prvega reda, linearne diferencialne enačbe prvega reda,

**Content (Syllabus outline):**

Selected topics in the following chapters are discussed.

- Functions of several variables. Definition and continuity, partial derivative, total differential, higher order partial derivatives, extrema, Taylor series.
- Differential equations. Basic notions, simple first order differential equations, first order linear differential equations, second order

linearne diferencialne enačbe drugega reda s konstantnimi koeficienti, sistemi linearnih diferencialnih enačb, uporaba diferencialnih enačb v biologiji in ekologiji.

- Osnovni pojmi teorije verjetnosti. Definicija verjetnosti in njene lastnosti. Pogojna verjetnost. Zaporedja neodvisnih poskusov. Naključne spremenljivke. Pomembne diskretne in zvezne porazdelitve.
- Analiza diskretnih in zveznih stohastičnih modelov. Zaporedje odvisnih poskusov: markovske verige. Klasifikacija stanj. Stacionarna porazdelitev. Primeri uporabe stohastičnih modelov v biologiji in ekologiji.

linear differential equations with constant coefficients, systems of linear differential equations, applying differential equations to problems in biology and ecology.

- Basic concepts of probability theory. The definition of probability and its properties. Conditional probability. Sequences of independent trials: Bernoulli trials. Random variables. Examples of the most important discrete and continuous distributions.
- Analyzing discrete and continuous stochastic models. Sequences of dependent trials: Homogeneous Markov chains. Classification of states. Stationary distribution. Examples of stochastic models in biology and ecology.

### Temeljni literatura in viri / Readings:

- Jamnik, R., 1987: Verjetnostni račun, DMFA, Ljubljana.
- Kot, M., 2001: Elements of Mathematical Ecology. Cambridge.
- Mizori-Oblak, P., 1986: Matematika za študente tehnike in naravoslovja, I-III, FS, Ljubljana.
- Otto, S., T. Day, 2006: A Biologist's Guide to Mathematical Modeling, Princeton University Press.
- Vidav, I, 1976: Višja matematika III, DZS, Ljubljana.

### Cilji in kompetence:

Predstaviti:

- Koncepti obravnave izbranih funkcij več realnih spremenljivk
- Teorijo diferencialnih enačb in njihovo uporabo v biologiji in ekologiji
- Izbrane koncepte verjetnostnega računa
- Teorijo stohastičnih procesov in njihovo uporabo v biologiji in ekologiji

### Objectives and competences:

To present:

- Concepts of the study of selected functions of several variables
- Theory of differential equations and to illustrate several applications of differential equations to problems in biology and ecology
- Selected concepts of the study of probability
- Theory of stochastic process and its application in biology and ecology

### Predvideni študijski rezultati:

#### Znanje in razumevanje:

Znanje in razumevanje:

- Poznavanje konceptov obravnave izbranih funkcij več realnih spremenljivk
- Prepoznavanje izbranih tipov diferencialnih

### Intended learning outcomes:

#### Knowledge and understanding:

Knowledge and Understanding:

- Understanding concepts of the study of selected functions of several variables
- Identifying selected types of differential

<p>enačb</p> <ul style="list-style-type: none"> <li>• Poznavanje izbranih metod reševanja diferencialnih enačb</li> <li>• Poznavanje izbranih primerov uporabe diferencialnih enačb v biologiji in ekologiji</li> <li>• Razumevanje izbranih konceptov verjetnosti, ki so povezani s naqključnimi procesi</li> <li>• Poznavanje izbranih primerov uporabe stohastičnih modelov v biologiji in ekologiji</li> </ul> <p><b>Prenesljive/ključne spretnosti in drugi atributi:</b></p> <ul style="list-style-type: none"> <li>• Pridobljeno znanje je prenesljivo na druga področja (biologija, ekologija, fizika, kemija, ekonomija,...)</li> </ul>	<p>equations,</p> <ul style="list-style-type: none"> <li>• Knowledge of selected methods for solving differential equations</li> <li>• Knowledge of applications of selected differential equations to problems in biology and ecology.</li> <li>• Understanding selected concepts of the probability theory which are related to stochastic process.</li> <li>• Knowledge of selected applications of stochastic models to problems in biology and ecology.</li> </ul> <p><b>Transferable/Key Skills and other attributes:</b></p> <ul style="list-style-type: none"> <li>• The obtained knowledge is transferable to other fields (biology, ecology, physics, chemistry, economics, ...).</li> </ul>
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**Metode poučevanja in učenja:**

<ul style="list-style-type: none"> <li>• Predavanja</li> <li>• Teoretične vaje</li> <li>• Konzultacije</li> </ul>
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**Learning and teaching methods:**

<ul style="list-style-type: none"> <li>• Lectures</li> <li>• Theoretical excersises</li> <li>• Consultations</li> </ul>
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**Načini ocenjevanja:**

Delež (v %) /  
Weight (in %)

**Assessment:**

<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt):</p> <p>Pisni test – praktični del Izpit (ustni) – teoretični del</p> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno. Pozitivna ocena pri pisnem testu je pogoj za pristop k izpitu.</p>	<p>50% / 50%</p>	<p>Type (examination, oral, coursework, project):</p> <p>Written test – practical part Exam (oral) – theoretical part</p> <p>Each of the mentioned commitments must be assessed with a passing grade. Passing grade of the written test is required for taking the exam.</p>
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**Reference nosilca / Lecturer's references:**

1. EREMITA, Daniel, GOGIĆ, Ilja, ILIŠEVIĆ, Dijana. Generalized skew derivations implemented by elementary operators. *Algebras and representation theory*, ISSN 1386-923X, 2014, vol. 17, iss. 3, str. 983-996. <http://dx.doi.org/10.1007/s10468-013-9429-8>. [COBISS.SI-ID [17043545](#)]
2. EREMITA, Daniel. Functional identities of degree 2 in triangular rings revisited. *Linear and Multilinear Algebra*, ISSN 0308-1087, 2014, 20 str. <http://dx.doi.org/10.1080/03081087.2013.877012>, doi: [10.1080/03081087.2013.877012](https://doi.org/10.1080/03081087.2013.877012). [COBISS.SI-ID [17044057](#)]
3. EREMITA, Daniel. Functional identities of degree 2 in triangular rings. *Linear Algebra and its Applications*, ISSN 0024-3795. [Print ed.], 2013, vol. 438, iss 1, str. 584-597. <http://dx.doi.org/10.1016/j.laa.2012.07.028>. [COBISS.SI-ID [16528217](#)]
4. EREMITA, Daniel, ILIŠEVIĆ, Dijana. On (anti-)multiplicative generalized derivations. *Glasnik matematički. Serija 3*, ISSN 0017-095X, 2012, vol. 47, no. 1, str. 105-118. <http://dx.doi.org/10.3336/gm.47.1.08>. [COBISS.SI-ID [16341849](#)]
5. BENKOVIČ, Dominik, EREMITA, Daniel. Multiplicative Lie n-derivations of triangular rings. *Linear Algebra and its Applications*, ISSN 0024-3795. [Print ed.], 2012, vol. 436, iss 11, str. 4223-4240. <http://dx.doi.org/10.1016/j.laa.2012.01.022>. [COBISS.SI-ID [16278361](#)]