



Univerza v Mariboru



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Fakulteta za naravoslovje in
matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Osnove teorije grafov
Course title:	Basic graph theory

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Izobraževalna matematika, dvopredmetni študij, 2. stopnja		2.	3.
Educational mathematics, double major 2 nd degree		2.	3.

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
15	15	15			45	3

Nosilec predmeta / Lecturer:

Jeziki / Languages:	Predavanja / Lectures:	<input type="text" value="SLOVENSKO/SLOVENE"/>
	Vaje / Tutorial:	<input type="text" value="SLOVENSKO/SLOVENE"/>

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Prerequisites:

Vsebina:

- Osnovni pojmi in primeri: graf, stopnja, izomorfizem grafov, podgrafi, povezanost, poti in cikli, dvodelni grafi, drevesa, tetivni grafi.
- Prirejanja: prirejanja in pokritja, prirejanja v dvodelnih grafih, prirejanja v splošnih grafih, Hallov poročni izrek.
- Ravninski grafi: risbe grafov, zemljevidi, dualni graf, Eulerjeva formula.

Content (Syllabus outline):

- Basic concepts and examples: graph, degree, graph isomorphism, subgraphs, paths and cycles, trees, bipartite graphs, chordal graphs.
- Matchings: matchings and covers, matchings in bipartite graphs, matchings in general graphs, Hall's marriage theorem,
- Planar graphs: graph drawings, maps, graph dual, Euler's formula,

- Barvanja grafov: barvanja vozlišč, Brooksov izrek, barvanja povezav, barvanja zemljevidov, izrek 4 barv, sodobni koncepti barvanj.
- Eulerjevi in Hamiltonovi grafi: problem Konnigsbergških mostov in Eulerjev izrek, Fleuryjev postopek, Hamiltonovi cikli in poti, potrebni in zadostni pogoji za hamiltonskost, usmerjeni grafi in turnirji, problem trgovskega potnika, problem kitajskega poštarja.

Del snovi bo prilagojen interesom in pobudam študentov ali sproti se porajajočim trendom v teoriji grafov in razvedrilni diskretni matematiki.

- Colourings of graphs: vertex colourings, Brooks' theorem, edge colourings, map colourings, 4 colour theorem, modern colouring concepts.
- Eulerian and hamiltonian graphs: bridges of Konnigsberg problem and Euler's theorem, Fleury's procedure, Hamilton cycles and paths, necessary and sufficient conditions for hamiltonicity, digraphs and tournaments, traveling salesman problem, Chinese postman problem.

A part of the contents will be adjusted to interests and initiative of students or to newly appearing trends in graph theory and recreational discrete mathematics.

Temeljni literatura in viri / Readings:

- D.B. West: *Introduction to Graph Theory*, Prentice Hall, New Jersey, 2001.
- R. J. Wilson, J. J. Watkins: *Uvod v teorijo grafov*, DMFA, Ljubljana, 1997.
- R. J. Wilson: *Introduction to graph theory*, Longman, New York, 1987.
- J.A. Bondy and U.S.R. Murty: *Graph Theory*, Springer, London, 2008.

Cilji in kompetence:

Cilj predmeta je seznaniti študente z najpomembnejšimi koncepti teorije grafov in njene uporabe. V okviru seminarja se študent samostojno nauči izbrano snov in pripravi seminarsko predstavitev.

Objectives and competences:

The objective of this course is to acquaint students with the most important concepts in graph theory and its application. For the seminar a student self-reliantly learns a chosen topic and prepares a presentation.

Predvideni študijski rezultati:

Znanje in razumevanje:
Po zaključku tega predmeta bo študent sposoben izkazati razumevanje osnov teorije grafov, reševati probleme, ki se v teoriji grafov pojavljajo ter pridobljeno znanje uporabljati.

Prenesljive/ključne spretnosti in drugi atributi:

- *Spretnosti komuniciranja*: ustno izražanje in javni nastop pri seminarju, ustno in pisno izražanje na izpitih
- *Reševanje problemov*: reševanje kombinatoričnih in ekstremalnih problemov v teoriji grafov.

Intended learning outcomes:

Knowledge and Understanding:
On completion of this course the student will be able to demonstrate understanding of graph theory basics, solve problems that appear in graph theory and apply the obtained knowledge.

Transferable/Key Skills and other attributes:

- *Communication skills*: public performance at seminar presentation, manner of expression at exams.
- *Problem solving*: solving combinatorial and extremal problems in graph theory.

Metode poučevanja in učenja:

- Predavanja

Learning and teaching methods:

- Lectures

<ul style="list-style-type: none"> • Seminar • Individualno delo 	<ul style="list-style-type: none"> • Seminar • Individual work 	
Načini ocenjevanja:	Assessment:	
<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt)</p> <p>Seminar</p> <p>Pisni izpit (naloge)</p> <p>Izpit (teorija)</p> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p> <p>Pozitivna ocena pri seminarju in pisnem izpitu sta pogoja za pristop k izpitu iz teorije</p>	<p>Delež (v %) / Weight (in %)</p> <p>30%</p> <p>30%</p> <p>40%</p>	<p>Type (examination, oral, coursework, project):</p> <p>Seminar</p> <p>Written Exam (exercises)</p> <p>Exam (theory)</p> <p>Each of the mentioned commitments must be assessed with a passing grade.</p> <p>Passing grade of the seminar and of the written are required for taking the exam.</p>
Reference nosilca / Lecturer's references:		
<p>1. BOKAL, Drago, BREŠAR, Boštjan, JEREBIC, Janja. A generalization of Hungarian method and Hall's theorem with applications in wireless sensor networks. <i>Discrete appl. math.</i>. [Print ed.], 2012, vol. 160, iss. 4-5, str. 460-470. http://dx.doi.org/10.1016/j.dam.2011.11.007. [COBISS.SI-ID 16191577]</p> <p>2. BREŠAR, Boštjan, CHALOPIN, Jérémie, CHEPOI, Victor, GOLOGRANC, Tanja, OSAJDA, Damian. Bucolic complexes. <i>Preprint series</i>, 2012, vol. 50, št. 1171, str. 1-24. http://www.imfm.si/preprinti/PDF/01171.pdf. [COBISS.SI-ID 16207961]</p> <p>3. BALAKRISHNAN, Kannan, BREŠAR, Boštjan, CHANGAT, Manoj, KLAVŽAR, Sandi, PETERIN, Iztok, SUBHAMATHI, Ajitha R. Almost self-centered median and chordal graphs. <i>Taiwan. j. math.</i>, 2012, vol. 16, no. 5, str. 1911-1922. http://journal.taiwanmathsoc.org.tw/index.php/TJM/article/view/2393/1403. [COBISS.SI-ID 16376409]</p> <p>4. BREŠAR, Boštjan, KARDOŠ, František, KATRENIČ, Ján, SEMANIŠIN, Gabriel. Minimum k-path vertex cover. <i>Discrete appl. math.</i>. [Print ed.], 2011, vol. 159, iss. 12, str. 1189-1195. http://dx.doi.org/10.1016/j.dam.2011.04.008. [COBISS.SI-ID 15929689]</p> <p>5. BREŠAR, Boštjan, KRANER ŠUMENJAK, Tadeja, TEPEH, Aleksandra. The geodetic number of the lexicographic product of graphs. <i>Discrete math.</i>. [Print ed.], 2011, vol. 311, iss. 16, str. 1693-1698. http://dx.doi.org/10.1016/j.disc.2011.04.004. [COBISS.SI-ID 15929945]</p>		