



Univerza v Mariboru

Fakulteta za naravoslovje
in matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Dinamični sistemi
Course title:	Dynamical Systems

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Dvopredmetna izobraževalna fizika	/	2	3
Double major Educational Physics	/		

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Lab. vaje Laboratory work	Terenske vaje Field work	Samost. delo Individ. work	ECTS
45			30		75	5

Nosilec predmeta / Lecturer:

Jeziki /	Predavanja / Lectures:	slovenski / slovene
Languages:	Vaje / Tutorial:	slovenski / slovene

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:
<input type="text" value="Predznanje analize, algebre, matematične fizike."/>	<input type="text" value="Preknowledge of calculus, algebra and mathematical physics."/>

Vsebina: **Content (Syllabus outline):**

1. Preprosti matematični opis dinamike sistema (enodimenzionalni (1D) sistemi)

Splošna definicija dinamičnih sistemov, avtonomnost dinamičnega sistema, fazni prostor, linearna stabilnostna analiza, bifurkacijska analiza, enodimenzionalni sistemi in oscilacije.

2. Dinamični sistemi in oscilacije (2D sistemi)

Linearni 2D sistemi, nelinearni 2D sistemi, linearizacija sistema in linearna stabilnostna analiza, konzervativni in disipativni sistemi, oscilator – konzervativni sistemi, oscilator – disipativni sistem, bifurkacije, bifurkacijski diagram, lokalne in globalne bifurkacije.

3. Kompleksni atraktorji (3D sistemi)

Fourierjeva transformacija in avtokorelacija, Lyapunovi eksponenti, regularni atraktorji v 3D, kaos, čudni atraktorji in fraktalne dimenzije.

4. Aplikacije

Pomen dinamičnih sistemov v fiziki in na drugih področjih: dinamični sistemi v biologiji, okoljevarstvu, ekonomiji,

5. Uporaba računalniških programov

Uporaba računalniških programov za implementacijo dinamičnih sistemov: DynaSys, Stella, Madonna, C++, ...

1. Basic mathematical description of the system dynamics (one-dimensional (1D) systems)

Definition of dynamical systems, autonomous dynamical systems, the phase space, the linear stability analysis, the bifurcation analysis, onedimensional systems and oscillations.

2. Dynamical systems and oscillations (2D systems)

Linear 2D systems, nonlinear 2D systems, linearization and linear stability analysis, conservative and dissipative systems, oscillator – conservative system, oscillator – dissipative system, bifurcations, bifurcation diagram, local and global bifurcations.

3. Complex attractors (3D systems)

Fourier transformation and autocorrelation, Lyapunov exponents, regular attractors in 3D, chaos, strange attractors and fractal dimensions.

4. Applications

The role of dynamical systems in physics and in other fields: dynamical systems in biology, environmental science, economy, ...

5. Using of computer programs

Computer programmes for the implementation of dynamical systems: DynaSys, Stella, Madonna, C++, ...

Temeljni literatura in viri / Readings:

- Steven H. Strogatz, *Nonlinear Dynamics and Chaos with Applications to Physics, Biology, Chemistry, and Engineering*. Perseus Pub., Cambridge, 1994.
- J. B. Snape, I. J. Dunn, J. Ingham, J. E. Prenosil, *Dynamics of Environmental Bioprocesses, Modelling and Simulation*, VCH Verlagsgesellschaft, Weinheim, 1995.
- Natali Hritonenko, Yuri Yatsenko, *Mathematical Modeling in Economics, Ecology and the Environment*, Springer, New York, 1999.
- Strokovni in znanstveni članki v revijah / Articles published in professional and scientific journals.

Cilji in kompetence:

- Razviti sposobnosti za opravljanje kvantitativne analize dinamike kompleksnih sistemov.
- Razumeti ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Poznati uporabnost znanja o dinamičnih sistemih v naravnih sistemih in prenos znanja na druga področja.
- Znati uporabiti računalniške programe za implementacijo dinamičnih sistemov.

Objectives and competences:

- Develop the skills for quantitative analysis of the dynamics of complex systems.
- Understand the basic differences and characteristics of dynamical systems in different dimensions.
- Know the applicability of knowledge about dynamical systems in the nature and the transfer of knowledge to other fields.
- Use computer programs for the implementation of dynamical systems.

Predvideni študijski rezultati:

Znanje in razumevanje:

- Usvojiti metode za kvantitativno analizo dinamike kompleksnih sistemov.
- Spoznati ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Spoznati uporabnost znanja o dinamičnih sistemih v fiziki in prenos znanja na druga področja.
- Znati uporabljati računalniške programe za implementacijo dinamičnih sistemov.

Intended learning outcomes:

Knowledge and Understanding:

- Be able to use methods for quantitative analysis of the dynamics of complex systems.
- Know basic differences and characteristics of dynamical systems in different dimensions.
- Be able to apply the knowledge about dynamical systems in physics to other fields.
- Using computer programs for the implementation of dynamical systems.

Prenesljive/ključne spretnosti in drugi atributi:

- Metode kvantitativne analize dinamičnih sistemov so univerzalne in jih je mogoče uporabiti na najrazličnejših področjih.
- Poudarek je na prenosu znanja s primerov iz fizike na področja biologije, ekologije, ekonomije, ...

Metode poučevanja in učenja:

- Predavanja
- Teoretične vaje
- Vaje na računalniku

Transferable/Key Skills and other attributes:

- Methods for quantitative analysis of dynamical system are universal and can be implemented in different fields of research.
- In particular, a knowledge transfer from examples in physics to examples in biology, ecology, economics, etc. is emphasised.

Learning and teaching methods:

- Lectures
- Theoretical exercises
- Computer exercises

Delež (v %) / oral exam, seminar

Načini ocenjevanja:

Weight (in %)

- ustni izpit	70	- oral exam
- seminarska naloga	30	- seminar

Reference nosilca / Lecturer's references:

Detecting chaos from a time series, Stane Kodba, Matjaž Perc and Marko Marhl, Eur. J. Phys. 26, 205-215 (2005)

Visualizing the attraction of strange attractors, Matjaž Perc, Eur. J. Phys. 26, 579-587 (2005)

Nonlinear time series analysis of the human electrocardiogram, Matjaž Perc, Eur. J. Phys. 26, 757-768 (2005)

The dynamics of human gait, Matjaž Perc, Eur. J. Phys. 26, 525-534 (2005)

Deterministic chaos in sounds of Asian cicadas, Tina P. Benko and Matjaž Perc, J. Biol. Syst. 14, 555-566 (2006)

The dynamics of laser droplet generation, Blaž Krese, Matjaž Perc and Edvard Govekar, Chaos 20, 013129 (2010)