



Univerza v Mariboru



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Fakulteta za naravoslovje in
matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Nelinearni dinamični sistemi
Course title:	Nonlinear Dynamical Systems

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Fizika 2. st.		1	2
Physics 2 nd degree		1	2

Vrsta predmeta / Course type Izbirni/optional

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
15		30				5

Nosilec predmeta / Lecturer: Marko Marhl

Jeziki / Languages:	Predavanja / Lectures:	slovenski/Slovenian in/and angleški/English
	Vaje / Tutorial:	slovenski/Slovenian in/and angleški/English

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Predznanje modelske fizike in fizike kompleksnih sistemov

Prerequisites:

Preknowledge of physics of complex systems and physics modelling

Vsebina:

Nelinearni dinamični sistemi v 1D, 2D in 3D
Linearizacija in linearna stabilnostna analiza, bifurkacijska analiza.

2. Nelinearni oscilatorji
Regularni oscilatorji kot konzervativni in disipativni sistemi (center, limitni cikel), bifurkacije, bifurkacijski diagram, lokalne in globalne bifurkacije.

3. Kvaziperiodičnost, kaos

Content (Syllabus outline):

Nonlinear dynamical systems (1D-, 2D-, 3D- systems)
Linearization and the linear stability analysis, the bifurcation analysis.

2. Nonlinear oscillators
Regular oscillators as conservative and dissipative systems (centre, limit cycle), bifurcations, bifurcation diagram, local and global bifurcations.

3. Quasiperiodicity, chaos

Fourierjeva transformacija in avtokorelacija, Lyapunovi eksponenti, kaos

4. Fraktali in fraktalne dimenzije.

5. Stohastično modeliranje (Gillespiev algoritem)

6. Aplikacije

Pomen dinamičnih sistemov v fiziki in na drugih področjih: dinamični sistemi v biologiji, okoljevarstvu, ekonomiji,

7. Uporaba računalniških programov

Uporaba računalniških programov za implementacijo dinamičnih sistemov: DynaSys, Stella, Madonna, C++, ...

Fourier transformation and autocorrelation, Lyapunov exponents.

4. Fractals and fractal dimension

5. Stochastic modelling (Gillespie's algorithm)

6. Applications

The role of dynamical systems in physics and in other fields: dynamical systems in biology, environmental science, economy, ...

7. Using of computer programs

Computer programmes for the implementation of dynamical systems: DynaSys, Stella, Madonna, C++, ...

Temeljni literatura in viri / Readings:

- Steven H. Strogatz, *Nonlinear Dynamics and Chaos with Applications to Physics, Biology, Chemistry, and Engineering*. Perseus Pub., Cambridge, 1994.
- J. B. Snape, I. J. Dunn, J. Ingham, J. E. Prenosil, *Dynamics of Environmental Bioprocesses, Modelling and Simulation*, VCH Verlagsgesellschaft, Weinheim, 1995.
- Natali Hritonenko, Yuri Yatsenko, *Mathematical Modeling in Economics, Ecology and the Environment*, Springer, New York, 1999.
- Strokovni in znanstveni članki v revijah / Articles published in professional and scientific journals.

Cilji in kompetence:

- Razvijati sposobnosti za opravljanje kvantitativne analize dinamike kompleksnih sistemov.
- Predstaviti ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Poudariti uporabnost znanja o dinamičnih sistemih v naravnih sistemih in prenos znanja na druga področja.
- Uporaba računalniških programov za implementacijo dinamičnih sistemov.

Objectives and competences:

- Developing skills for quantitative analysis of the dynamics of complex systems.
- Presenting basic differences and characteristics of dynamical systems in different dimensions.
- Pointing out the applicability of knowledge about dynamical systems in the nature and the transfer of knowledge to other fields.
- Using computer programs for the implementation of dynamical systems.

Predvideni študijski rezultati:

Znanje in razumevanje:

- Usvojiti metode za kvantitativno analizo dinamike kompleksnih sistemov.
- Spoznati ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Pomen determinističnega in stohastičnega modeliranja.
- Spoznati uporabnost znanja o dinamičnih sistemih v fiziki in prenos znanja na druga področja.
- Znati uporabljati računalniške programe za implementacijo dinamičnih sistemov.

Prenosljive/ključne spretnosti in drugi atributi:

- Metode kvantitativne analize dinamičnih sistemov so univerzalne in jih je mogoče uporabiti na najrazličnejših področjih.
- Poudarek je na prenosu znanja s primerov iz fizike na področja biologije, ekologije, ekonomije, ...

Intended learning outcomes:

Knowledge and Understanding:

- Be able to use methods for quantitative analysis of the dynamics of complex systems.
- Know basic differences and characteristics of dynamical systems in different dimensions.
- Importance of deterministic and stochastic modelling.
- Be able to apply the knowledge about dynamical systems in physics to other fields.
- Using computer programs for the implementation of dynamical systems.

Transferable/Key Skills and other attributes:

- Methods for quantitative analysis of dynamical system are universal and can be implemented in different fields of research.

In particular, a knowledge transfer from examples in physics to examples in biology, ecology, economics, etc. is emphasised.

Metode poučevanja in učenja:

- Predavanja
- Teoretične vaje
- Vaje na računalniku
- Seminarske vaje

Learning and teaching methods:

- Lectures
- Theoretical exercises
- Computer exercises
- Seminar

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Načini ocenjevanja:	Delež (v %) / Weight (in %)	Assessment:
<ul style="list-style-type: none"> • ustni izpit • pisni izpit • projektna naloga 	40 40 20	<ul style="list-style-type: none"> • oral exam • written exam • projektna naloga

Reference nosilca / Lecturer's references:

BODENSTEIN, Christian, GOSAK, Marko, SCHUSTER, Stefan, MARHL, Marko, PERC, Matjaž. Modeling the seasonal adaptation of circadian clocks by changes in the network structure of the suprachiasmatic nucleus. *PLOS comput. biol.*, Sep. 2012, vol. 8, iss. 9, e1002697-1-e1002697-12.

MARHL, Marko, GOSAK, Marko, PERC, Matjaž, ROUX, Etienne. Importance of cell variability for calcium signaling in rat airway myocytes. *Biophysical chemistry*. [Print ed.], 2010, vol. 148, iss. 1/3, str. 42-50.

GOSAK, Marko, KOROŠAK, Dean, MARHL, Marko. Optimal network configuration for maximal coherence resonance in excitable systems. *Phys. rev., E Stat. nonlinear soft matter phys. (Print)*, 2010, vol. 81, iss. 5, str. 056104-1-056104-7.

GRUBELNIK, Vladimir, DUGONIK, Bogdan, OSEBIK, Davorin, MARHL, Marko. Signal amplification in biological and electrical engineering systems : universal role of cascades. *Biophysical chemistry*. [Print ed.], aug. 2009, vol. 143, iss. 3, str. 132-138.

MARHL, Marko, GOSAK, Marko, PERC, Matjaž, DIXON, C. Jane, GREEN, Anne K. Spatio-temporal modelling explains the effect of reduced plasma membrane Ca²⁺ efflux on intracellular Ca²⁺ oscillations in hepatocytes. *J. theor. biol.*, 2008, vol. 252, iss. 3, str. 419-426.