



Univerza v Mariboru

Fakulteta za naravoslovje  
in matematiko

**UČNI NAČRT PREDMETA / COURSE SYLLABUS**

<b>Predmet:</b>	Numerična analiza
<b>Course title:</b>	Numerical Analysis

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Matematika, 2. stopnja		1. ali 2.	2. ali 4.
Mathematics, 2 <sup>nd</sup> degree		1. or 2.	2. ali 4.

**Vrsta predmeta / Course type**

**Univerzitetna koda predmeta / University course code:**

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
60		30	15		195	10

**Nosilec predmeta / Lecturer:**

<b>Jeziki / Languages:</b>	<b>Predavanja / Lectures:</b>	SLOVENSKO/SLOVENE
	<b>Vaje / Tutorial:</b>	SLOVENSKO/SLOVENE

**Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:** **Prerequisites:**

**Vsebina:**

1. Analize numeričnega računanja.
2. Reševanje nelinearnih enačb: Reševanje sistemov nelinearnih enačb.
3. Diferenčne operatorji in diferenčne enačbe.
4. Sistemi linearnih enačb. Iterativne metode.
5. Problem lastnih vrednosti: Schurov in Gershgorinov izrek. Simetrični in nesimetrični problem lastnih vrednosti.
6. Navadne diferencialne enačbe: Lastnosti rešitev in stabilnost rešitev. Picardova

**Content (Syllabus outline):**

1. Analysis of numerical computing.
2. Nonlinear equations solving: Systems of nonlinear equations.
3. Difference equations and difference operators.
4. Systems of linear equations. Iterative methods.
5. Eigenvalues computation problem: Schur's and Gershgorin's theorems. Symmetric and non-symmetric eigenvalue problem.

<p>metoda. Metode Runge-Kutta. Večkoračne metode. Robni problem. Sistemi diferencialnih enačb.</p> <p>7. Numerično odvajanje: Richardsonova ekstrapolacija.</p> <p>8. Polinomske sistemi: Groebnerjeva baza. Raznoterost polinomskega ideala in njene lastnosti. Razcep raznoterosti.</p> <p>9. Parcialne diferencialne enačbe.</p>	<p>6. Ordinary differential equations: Properties of solutions and stability of solutions. Runge-Kutta methods. Multi-step methods. Boundary-value problems. Systems of differential equations.</p> <p>7. Numeric derivation: Richardson's extrapolation.</p> <p>8. Polynomial systems: Groebner basis, Variety of polynomial ideal and its properties. Decomposition of varieties. Modular methods.</p> <p>9. Partial differential equations.</p>
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### Temeljni literatura in viri / Readings:

Z. Bohte, Numerično reševanje nelinearnih enačb, DMFA Slovenije, Ljubljana, 1993.  
 Z. Bohte, Numerično reševanje sistemov linearnih enačb, DMFA Slovenije, Ljubljana, 1994.  
 D. Kincaid, W. Cheney: Numerical Analysis, Brooks/Cole, Pacific Grove, 1996.  
 E. Zakrajšek, Uvod v numerične metode, druga izdaja, DMFA Slovenije, Ljubljana, 2000.  
 V. G. Romanovski and Douglas S. Shafer, The Center and Cyclicity Problems. A Computational Algebra Approach, Boston-Basel-Berlin: Birkhauser, 2009.  
 G. Teschl, Ordinary Differential Equations and Dynamical Systems. Providence: American Mathematical Society, 2012.

### Cilji in kompetence:

Poglobiti znanje iz zahtevnejših konceptov in rezultatov s področja numerične analize – simbolnega računanja in numeričnih metod.

### Objectives and competences:

To deepen the knowledge of more demanding concepts and results from numerical analysis – symbolic mathematics and numerical methods.

### Predvideni študijski rezultati:

Znanje in razumevanje:

- Poglobiti znanje iz zahtevnejših numeričnih metode in njihovih uporabnih vrednosti.
- Prepoznati praktične probleme in njihovo modeliranje z orodji numerične matematike.

Prenosljive/ključne spretnosti in drugi atributi:

- Prenos znanja numeričnih metod na druga področja (računalništvo, statistika, optimizacija, ...)

### Intended learning outcomes:

Knowledge and Understanding:

- To deepen the knowledge of more demanding numerical methods and their applications.
- To recognize practical problems and their modeling with numerical mathematics tools.

Transferable/Key Skills and other attributes:

- Knowledge transfer of numerical methods into other fields (computer science, statistics, optimization, ...)

### Metode poučevanja in učenja:

- Predavanja

### Learning and teaching methods:

- Lectures

<ul style="list-style-type: none"> <li>• Seminarske vaje</li> <li>• Izdelava seminarske naloge</li> </ul>	<ul style="list-style-type: none"> <li>• Tutorial</li> <li>• Seminar (project) work</li> </ul>	
<b>Načini ocenjevanja:</b>	<b>Assessment:</b>	
<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt)</p> <ul style="list-style-type: none"> <li>• Opravljena seminarska naloga</li> <li>• Pisni izpit – problemi</li> <li>• Pisni izpit – teoretija</li> </ul> <p>Pisni izpit - problemi se lahko nadomesti z dvema delnima testoma (sprotni obveznosti)</p> <p>Pisni izpit - teorija se lahko nadomesti z dvema delnima testoma (sprotni obveznosti)</p> <p>Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno.</p>	<p>Delež (v %) / Weight (in %)</p> <p>10%</p> <p>50%</p> <p>40%</p>	<p>Type (examination, oral, coursework, project):</p> <ul style="list-style-type: none"> <li>• Completed seminar (project) work</li> <li>• Written exam – problems</li> <li>• Written exam – theory</li> </ul> <p>Written exam – problems can be replaced by two parital tests (mid-term testing)</p> <p>Written exam – theory can be replaced by two parital tests (mid-term testing)</p> <p>Each of the mentioned commitments must be assessed with a passing grade.</p>
<b>Reference nosilca / Lecturer's references:</b>		
<p><b>1.</b> ROMANOVSKI, Valery, SHAFER, Douglas. <i>The center and cyclicity problems : a computational algebra approach</i>. Basel: Birkhäuser, 2009. XV; 330 str. ISBN 978-0-8176-4726-1. [COBISS.SI-ID <a href="#">62709761</a>]</p> <p><b>2.</b> ROMANOVSKI, Valery, PREŠERN, Mateja. An approach to solving systems of polynomials via modular arithmetics with applications. <i>Journal of Computational and Applied Mathematics</i>, ISSN 0377-0427. [Print ed.], 2011, vol. 236, iss. 2, str. 196-208. doi: <a href="#">10.1016/j.cam.2011.06.018</a>. [COBISS.SI-ID <a href="#">18552584</a>]</p> <p><b>3.</b> PAUSCH, Marina, GROSSMANN, Florian, ECKHARDT, Bruno, ROMANOVSKI, Valery. Groebner basis methods for stationary solutions of a low-dimensional model for a shear flow. <i>Journal of nonlinear science</i>, ISSN 0938-8974. [Print ed.], 2014, vol. 24, iss. 5, str. 935-948, doi: <a href="#">10.1007/s00332-014-9208-7</a>. [COBISS.SI-ID <a href="#">20920584</a>]</p> <p><b>4.</b> MAHDI, Adam, ROMANOVSKI, Valery, SHAFER, Douglas. Stability and periodic oscillations in the Moon-Rand systems. <i>Nonlinear analysis: real world applications</i>, ISSN 1468-1218, 2013, vol. 14, iss. 1, str. 294-313. [COBISS.SI-ID <a href="#">19482120</a>]</p> <p><b>5.</b> BOULIER, F., HAN, M., LEMAIRE, F., ROMANOVSKI, V. Qualitative investigation of a gene model using computer algebra algorithms. <i>Programming and computer software</i>, ISSN 0361-7688, 2015, vol. 41, no. 2, str. 105-111, doi: <a href="#">10.1134/S0361768815020048</a>. [COBISS.SI-ID <a href="#">21355784</a>]</p>		