

## UČNI NAČRT PREDMETA / COURSE SYLLABUS

<b>Predmet:</b>	Nelinearni dinamični sistemi
<b>Course title:</b>	Nonlinear Dynamical Systems

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Fizika 2. st.		1,2	2,3
Physics 2 <sup>nd</sup> degree		1,2	2,3

**Vrsta predmeta / Course type** izbirni/ optional

**Univerzitetna koda predmeta / University course code:**  

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
30	0	30	0	0	90	5

**Nosilec predmeta / Lecturer:** Marko Marhl

<b>Jeziki / Languages:</b>	<b>Predavanja / Lectures:</b>	slovenski/Slovenian in/and angleški/English
	<b>Vaje / Tutorial:</b>	slovenski/Slovenian in/and angleški/English

**Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:**

Predznanje modelske fizike in fizike kompleksnih sistemov

**Prerequisites:**

Preknowledge of physics of complex systems and physics modelling

**Vsebina:**

- 1. Nelinearni dinamični sistemi v 1D, 2D in 3D**  
Linearizacija in linearna stabilnostna analiza, bifurkacijska analiza.
- 2. Nelinearni oscilatorji**  
Regularni oscilatorji kot konzervativni in disipativni sistemi (center, limitni cikel), bifurkacije, bifurkacijski diagram, lokalne in globalne bifurkacije.
- 3. Kvaziperiodičnost, kaos**  
Fourierjeva transformacija in avtokorelacija, Lyapunovi eksponenti, kaos
- 4. Fraktali in fraktalne dimenzije.**
- 5. Stohastično modeliranje** (Gillespiev algoritem)
- 6. Aplikacije**  
Pomen dinamičnih sistemov v fiziki in na drugih področjih: dinamični sistemi v biologiji, okoljevarstvu, ekonomiji, ....
- 7. Uporaba računalniških programov**  
Uporaba računalniških programov za implementacijo dinamičnih sistemov: DynaSys, Stella, Madonna, C++, ...

**Content (Syllabus outline):**

- 1. Nonlinear dynamical systems (1D-, 2D-, 3D-systems)**  
Linearization and the linear stability analysis, the bifurcation analysis.
- 2. Nonlinear oscillators**  
Regular oscillators as conservative and dissipative systems (centre, limit cycle), bifurcations, bifurcation diagram, local and global bifurcations.
- 3. Quasiperiodicity, chaos**  
Fourier transformation and autocorrelation, Lyapunov exponents.
- 4. Fractals and fractal dimension**
- 5. Stochastic modelling** (Gillespie's algorithm)
- 6. Applications**  
The role of dynamical systems in physics and in other fields: dynamical systems in biology, environmental science, economy, ...
- 7. Using of computer programs**  
Computer programmes for the implementation of dynamical systems: DynaSys, Stella, Madonna, C++, ...

**Temeljni literatura in viri / Readings:**

1. Steven H. Strogatz, *Nonlinear Dynamics and Chaos with Applications to Physics, Biology, Chemistry, and Engineering*. Perseus Pub., Cambridge, 1994.
2. J. B. Snape, I. J. Dunn, J. Ingham, J. E. Prenosil, *Dynamics of Environmental Bioprocesses, Modelling and Simulation*, VCH Verlagsgesellschaft, Weinheim, 1995.
3. Natali Hritonenko, Yuri Yatsenko, **Mathematical Modeling in Economics, Ecology and the Environment**, Springer, New York, 1999.
4. Strokovni in znanstveni članki v revijah / Articles published in professional and scientific journals.

**Cilji in kompetence:**

- Razvijati sposobnosti za opravljanje kvantitativne analize dinamike kompleksnih sistemov.
- Predstaviti ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Poudariti uporabnost znanja o dinamičnih sistemih v naravnih sistemih in prenos znanja na druga področja.
- Uporaba računalniških programov za implementacijo dinamičnih sistemov.

**Objectives and competences:**

- Developing skills for quantitative analysis of the dynamics of complex systems.
- Presenting basic differences and characteristics of dynamical systems in different dimensions.
- Pointing out the applicability of knowledge about dynamical systems in the nature and the transfer of knowledge to other fields.
- Using computer programs for the implementation of dynamical systems.

**Predvideni študijski rezultati:**

## Znanje in razumevanje:

- Usvojiti metode za kvantitativno analizo dinamike kompleksnih sistemov.
- Spoznati ključne razlike in karakteristike dinamičnih sistemov v različnih dimenzijah.
- Pomen determinističnega in stohastičnega modeliranja.
- Spoznati uporabnost znanja o dinamičnih sistemih v fiziki in prenos znanja na druga področja.
- Znati uporabljati računalniške programe za implementacijo dinamičnih sistemov.

## Prenesljive/ključne spretnosti in drugi atributi:

- Metode kvantitativne analize dinamičnih sistemov so univerzalne in jih je mogoče uporabiti na najrazličnejših področjih.
- Poudarek je na prenosu znanja s primerov iz fizike na področja biologije, ekologije, ekonomije, ...

**Intended learning outcomes:**

## Knowledge and Understanding:

- Be able to use methods for quantitative analysis of the dynamics of complex systems.
- Know basic differences and characteristics of dynamical systems in different dimensions.
- Importance of deterministic and stochastic modelling.
- Be able to apply the knowledge about dynamical systems in physics to other fields.
- Using computer programs for the implementation of dynamical systems.

## Transferable/Key Skills and other attributes:

- Methods for quantitative analysis of dynamical system are universal and can be implemented in different fields of research.
- In particular, a knowledge transfer from examples in physics to examples in biology, ecology, economics, etc. is emphasised.

**Metode poučevanja in učenja:**

- Predavanja
- Teoretične vaje
- Vaje na računalniku
- Eksperimentalne vaje

**Learning and teaching methods:**

- Lectures
- Theoretical exercises
- Computer exercises
- Experiments

**Načini ocenjevanja:**Delež (v %) /  
Weight (in %)**Assessment:**

<ul style="list-style-type: none"> <li>• ustno</li> <li>• pisno</li> <li>• praktično - seminar</li> </ul>	40 40 20	<ul style="list-style-type: none"> <li>• oral</li> <li>• written</li> <li>• practical - seminar</li> </ul>
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**Reference nosilca / Lecturer's references:**

BODENSTEIN, Christian, KNOKE, Beate, MARHL, Marko, PERC, Matjaž, SCHUSTER, Stefan. Using Jensen's inequality to explain the role of regular calcium oscillations in protein activation. *Physical biology*, 2010, vol. 7, no. 3, str. 036009-1-036009-12, doi: [10.1088/1478-3975/7/3/036009](https://doi.org/10.1088/1478-3975/7/3/036009). [COBISS.SI-ID [14376470](https://www.cobiss.si/id/14376470)]

GOSAK, Marko, KOROŠAK, Dean, MARHL, Marko. Optimal network configuration for maximal coherence resonance in excitable systems. *Phys. rev., E Stat. nonlinear soft matter phys. (Print)*, 2010, vol. 81, iss. 5, str. 056104-1-056104-7, ilustr., doi: [10.1103/PhysRevE.81.056104](https://doi.org/10.1103/PhysRevE.81.056104). [COBISS.SI-ID [17626120](https://www.cobiss.si/id/17626120)]

KNOKE, Beate, BODENSTEIN, Christian, MARHL, Marko, PERC, Matjaž, SCHUSTER, Stefan. Jensen's inequality as a tool for explaining the effect of oscillations on the average cytosolic calcium concentration. *Theory biosci.*, Jun. 2010, vol. 129, no. 1, str. 25-38, doi: [10.1007/s12064-010-0080-1](https://doi.org/10.1007/s12064-010-0080-1). [COBISS.SI-ID [14376726](https://www.cobiss.si/id/14376726)]

GOSAK, Marko, KOROŠAK, Dean, MARHL, Marko. Topologically determined optimal stochastic resonance responses of spatially embedded networks. *New journal of physics*. [Online ed.], Jan. 2011, vol. 13, issue 1, str. 013012-1-013012-15, ilustr. <http://dx.doi.org/10.1088/1367-2630/13/1/013012>. [COBISS.SI-ID [18087432](https://www.cobiss.si/id/18087432)]

GOSAK, Marko, MARKOVIČ, Rene, MARHL, Marko. The role of neural architecture and the speed of signal propagation in the process of synchronization of bursting neurons. *Physica, A*. [Print ed.], 2012, vol. 391, no. 8, str. 2764-2770, ilustr., doi: [10.1016/j.physa.2011.12.027](https://doi.org/10.1016/j.physa.2011.12.027). [COBISS.SI-ID [18948872](https://www.cobiss.si/id/18948872)]