



Univerza v Mariboru



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Fakulteta za naravoslovje in
matematiko

UČNI NAČRT PREDMETA / COURSE SYLLABUS

Predmet:	Ravninska in prostorska geometrija
Course title:	Plane and solid geometry

Študijski program in stopnja Study programme and level	Študijska smer Study field	Letnik Academic year	Semester Semester
Izobraževalna matematika – dvopredmetni, 1. stopnja		2.	3.
Educational mathematics – Double-major, 1 st degree		2.	3.

Vrsta predmeta / Course type

Univerzitetna koda predmeta / University course code:

Predavanja Lectures	Seminar Seminar	Sem. vaje Tutorial	Lab. vaje Laboratory work	Teren. vaje Field work	Samost. delo Individ. work	ECTS
45		30	15		90	6

Nosilec predmeta / Lecturer:

**Jeziki /
Languages:**

**Predavanja /
Lectures:** SLOVENSKO/SLOVENE
Vaje / Tutorial: SLOVENSKO/SLOVENE

Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:

Prerequisites:

Vsebina:

Trikotnik. Cevov izrek. Znamenite točke trikotnika. Eulerjeva premica, krožnica devetih točk. Simsonova premica, Ptolomejev izrek.

Krožnica. Potenca točke glede na krožnico, potenčna premica in potenčno središče. Eulerjev izrek.

Content (Syllabus outline):

Triangle. Ceva's theorem. Basic triangle centers. Euler line, Nine-point circle. Simson line, Ptolemy's theorem.

Circle. Power of a point with respect to a circle, radical axis, radical center. Euler's theorem.

Quadrangles. Varignon's theorem. Cyclic

Štirikotniki. Varignonov izrek. Tetivni štirikotniki. Napoleonovi trikotniki. Ploščina. Brahmaguptova in Heronova formula.

Menelajev izrek in primeri uporabe.

Transformacije ravnine: izometrije (translacije, rotacije, zrcaljenja), raztegi. Inverzija.

Telesa. Prizma, piramida, valj, stožec, krogla. Volumen. Koti v telesih. Prostorski kot. Eulerjeva formula. Pravilna telesa.

quadrangles. Napoleon triangles. Area. Brahmagupta's formula. Heron's formula.

Menelaus' theorem and applications.

Transformations: isometries (translation, rotation, reflection), dilatation. Inversion.

Solid. Prism, Cylinder, Cone, Sphere. Volume. Angles in solids. Solid angles. Euler polyhedral formula. Platonic solids.

Temeljni literatura in viri / Readings:

H. S. M. Coxeter, S. L. Greitzer: *Geometry Revisited*. Washington: MAA, 1967.

C. Kimberling, *Geometry in action, a discovery approach using the Geometer's sketchpad*, Key College Publishing, Emeryville, 2003.

D. Palman: *Trokut i kružnica*. Zagreb: Element, 1994.

D. Palman: *Geometrijske konstrukcije*. Zagreb: Element, 1996.

D. Palman: *Stereometrija*. Zagreb: Element, 2002.

Bogomolny, A. "Regular Polyhedra." http://www.cut-the-knot.com/do_you_know/polyhedra.html.

Cilji in kompetence:

Študent se seznani z osnovami pojmi in rezultati geometrije trikotnika, s transformacijami v ravnini in njihovo uporabo pri geometrijskih konstrukcijah ter z osnovnimi pojmi prostorske geometrije.

Objectives and competences:

Knowing fundamental concepts and results from triangle geometry. Understanding transformations of the plane and their applications to geometric constructions. Knowing fundamental results from solid geometry.

Predvideni študijski rezultati:

Znanje in razumevanje:

- Študent obvlada pojme in rezultate iz ravninske in prostorske geometrije v razširjenem srednješolskem obsegu.
- Študent vadi dokazovanje trditev iz ravninske geometrije in s tem spoznava drugačen, manj računski pristop k dokazovanju.
- Študent obvlada osnovne geometrijske konstrukcije, tako z uporabo klasičnih orodij, kot z uporabo računalniških geometrijskih orodij.

Intended learning outcomes:

Knowledge and Understanding:

- Enlarging student's high school knowledge about the concepts and results from plane and solid geometry.
- Practicing the geometrical, noncomputational approach to proving results in plane geometry.
- Being able to accomplish basic geometric constructions applying classical tools as well as modern geometric computer tools.
- Understanding the importance of transformations of the plane mapping

- Študent spoznava pomen transformacij, ki konkretne geometrijske situacije preslikajo v bolj ugodne. Prenesljive/ključne spretnosti in drugi atributi: - Problemski pristop, kjer z računalniškim eksperimentiranjem tvorimo hipoteze in jih kasneje bodisi dokažemo bodisi ovržemo s protiprimi. - Dojemanje transformacij kot opcije za pretvorbo matematične situacije v drugo situacijo, ki je udobnejša za obravnavo.	geometric configurations into more convenient ones. Transferable/Key Skills and other attributes: - Problem solving approach, consisted of computer experimentation, proposing hypothesis and finding either the proof or the counterexample. - Understanding the concept of transformations as tools to convert a certain mathematical situation into a more convenient one.	
Metode poučevanja in učenja: - Predavanja - Teoretične vaje - Laboratorijske vaje v računalniški učilnici - Individualno delo	Learning and teaching methods: - Lectures - Theoretical exercises - Excercises in computer room. - Individual work	
Načini ocenjevanja:	Assessment:	
Način (pisni izpit, ustno izpraševanje, naloge, projekt) Pisni test – praktični del Izpit (ustni) – teoretični del Vsaka izmed naštetih obveznosti mora biti opravljena s pozitivno oceno. Pozitivna ocena pri pisnem testu je pogoj za pristop k izpitu.	Delež (v %) / Weight (in %) 50% 50%	Type (examination, oral, coursework, project): Written test – practical part Exam (oral) – theoretical part Each of the mentioned commitments must be assessed with a passing grade. Passing grade of the written test is required for taking the exam.
Reference nosilca / Lecturer's references:		
1. HVALA, Bojan. Diophantine Steiner triples. <i>Math. Gaz.</i>, March 2011, vol. 95, no. 532, str. 31-39. [COBISS.SI-ID 18256648] 2. HVALA, Bojan. Diophantine Steiner triples and Pythagorean-type triangles. <i>Forum geom.</i>, 2010, vol. 10, str. 93-97. http://forumgeom.fau.edu/FG2010volume10/FG201010.pdf. [COBISS.SI-ID 15669337] 3. HVALA, Bojan. Modernizing mathematics education in Slovenia : a teacher friendly approach. V: LAMANAUSKAS, Vincentas (ur.). <i>Challenges of science, mathematics and technology teacher</i>		

education in Slovenia, (Problems of education in the 21st century, vol. 14). Siauliai: Scientific Methodological Center Scientia Educologica, 2009, str. 34-43. [COBISS.SI-ID [17351944](#)]

4. HVALA, Bojan. Generalized Lie derivations in prime rings. *Taiwan. j. math.*, dec. 2007, vol. 11, iss. 5, str. 1425-1430. [COBISS.SI-ID [15969288](#)]

5. BREŠAR, Matej, HVALA, Bojan. On additive maps of prime rings. II. *Publ. math. (Debr.)*, 1999, letn. 54, št. 1/2, str. 39-54. [COBISS.SI-ID [8598617](#)]